

Test Bank for Thinking Quantitatively - Communicating with Numbers 3rd Gaze

INSTRUCTOR'S GUIDED WORKSHEETS

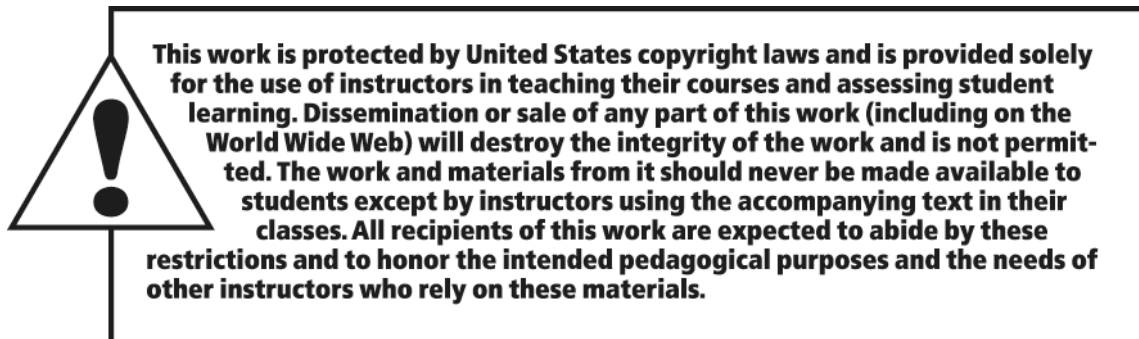
THINKING QUANTITATIVELY COMMUNICATING WITH NUMBERS

THIRD EDITION

Eric Gaze

Bowdoin College





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Quantitative Reasoning / Quantitative Literacy Worksheet

Why go to college? What is the PURPOSE of a college education? List 3 specific purposes:

1. *Career (#1 for students)*
2. *Life Skills*
3. *Critical Thinking (#1 for faculty)*

What is critical thinking? List 3 *characteristics* of critical thinking:

1. *Asking informed questions!*
2. *Weighing both sides of an argument.*
3. *Recognize and define problems.*

Summary

The purpose of this course is to give you the skills needed to make informed decisions when confronted with quantitative information in your personal, public, and professional lives. This introductory worksheet is simply meant to present you with quantitative information being presented as graphics like you will encounter in the popular press and in your courses.

At this point you are not expected to have the skills to answer the questions! They are meant to highlight how quantitative reasoning requires a different way of thinking and problem solving than is typically taught in traditional math courses. Try your best, work with your peers, and resolve to diligently work through the material in this course so that you will be among the few, the proud, the quantitatively literate :O)

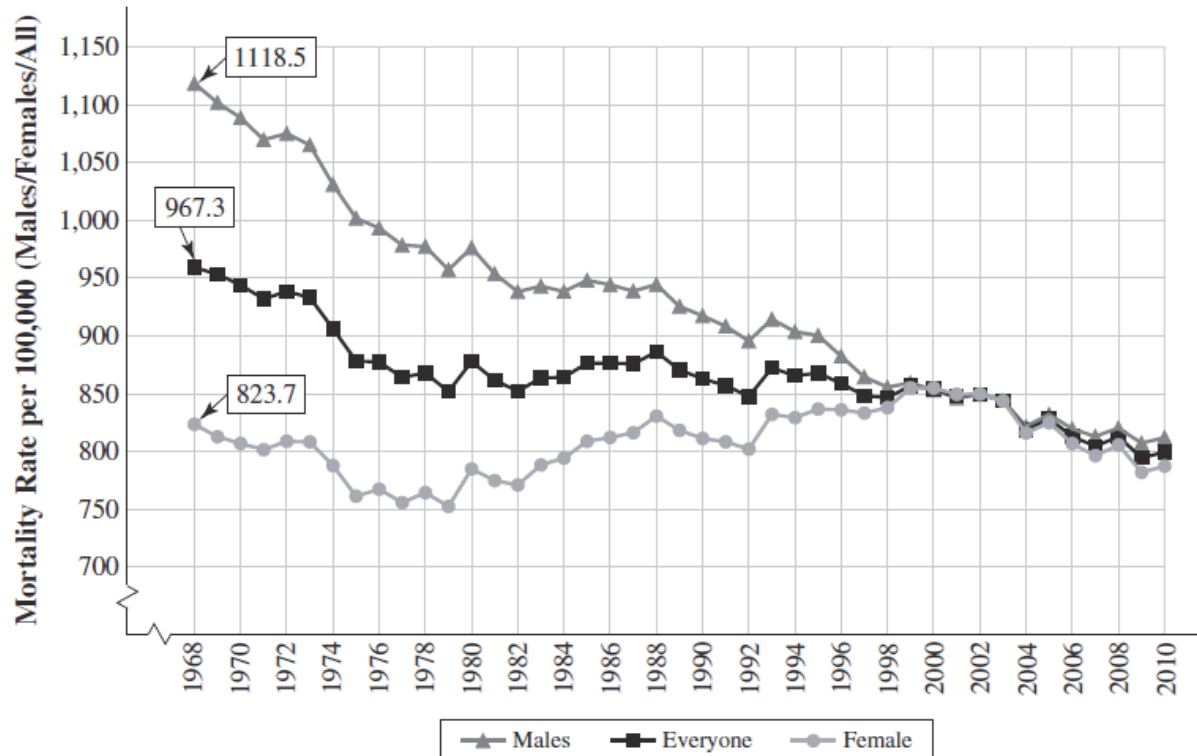
A piece presented in the Bloomberg View explores the data regarding “How Americans Die.”

<https://www.bloomberg.com/graphics/dataview/how-americans-die/>

Let’s take a closer look.

It may be helpful to have the slideshow open by opening the link when going over this in class.

1. On the first graph below use the statistics for 1968: 823.7, 967.3, and 1,118.5, in sentences.



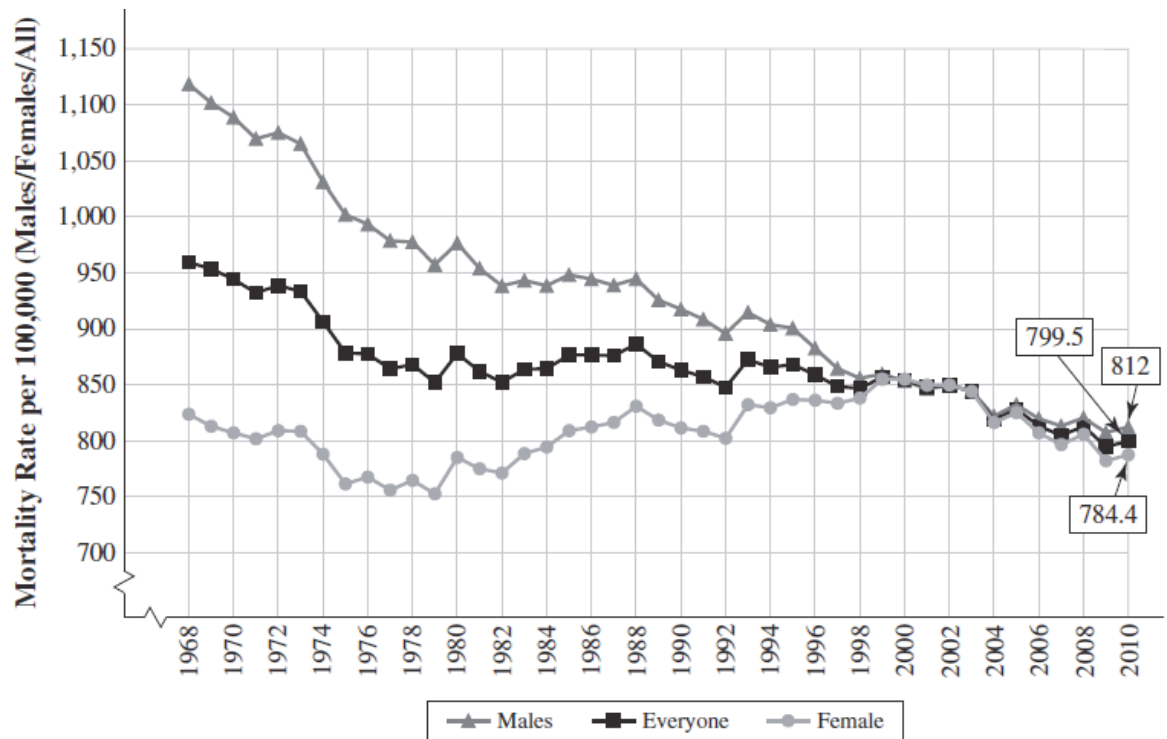
Data from: <http://www.bloomberg.com/dataview/2014-04-17/how-americans-die.html>

The mortality rate for the entire U.S. population in 1968 was 967.3 deaths per 100,000 people.

The mortality rate for U.S. women in 1968 was 823.7 deaths per 100,000 women.
The mortality rate for U.S. men in 1968 was 1,118.5 deaths per 100,000 men.

Note the second quantity of this ratio is not always people! If it was you could add the male and female rates to get the total. Also note the 967.3 is not the average of the male and female rates, there are more women in the population so the overall rate skews towards the female rate.

2. They tell us the overall rate “fell by about 17%” from 1968 to 2010, from 967.3 to 799.5.
 - a. Verify this and quantify the change for the rates for men and women in a similar fashion.



Data from: <http://www.bloomberg.com/dataview/2014-04-17/how-americans-die.html>

The total change is $799.5 - 967.3 = -167.8$, divide this by the original 967.3 to get -17.3% .

The total change is $784.4 - 823.7 = -39.3$, divide this by the original 823.7 to get -4.8% for women.

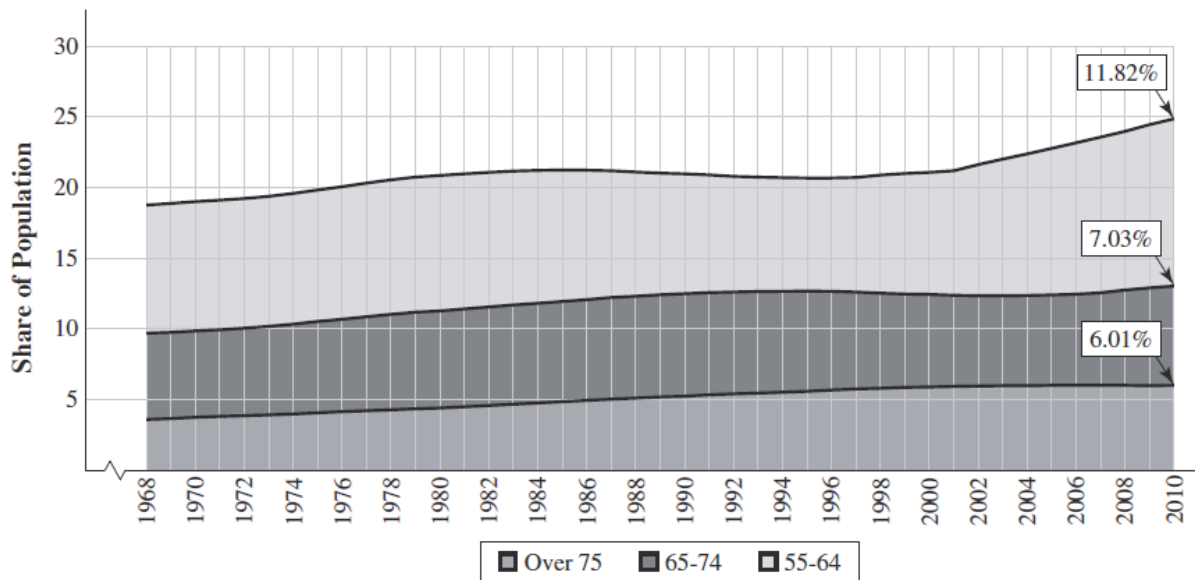
The total change is $812 - 1,118.5 = -306.5$, divide this by the original 1,118.5 to get -27.4% for men.

- b. Why can we compare the 1970 and 2010 statistics, even though the population has increased over this period?

Because we are using rates per 100,000 which take into the population sizes.

3. The slide associated with the first graph above says the decline in mortality rates stops in the mid 1990's and second slide with the graph below attributes this to the aging of the population.

a. What is the logic behind this argument?



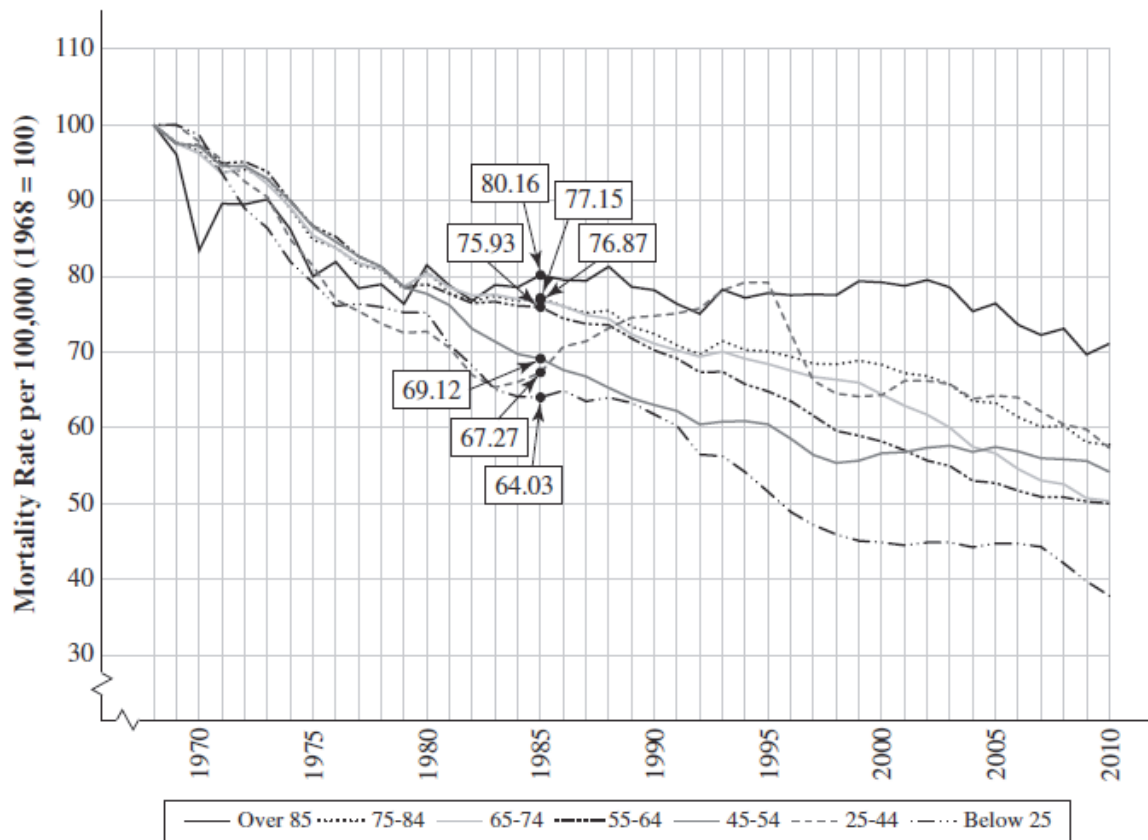
Data from: <http://www.bloomberg.com/dataview/2014-04-17/how-americans-die.html>

The aging population refers to a growing proportion of seniors in the population from 18.76% (from the slideshow but ~19%) 55 and older in 1968 to 24.86% (~25%) in 2010. So people living longer would first drive mortality rates down, but as we get a higher proportion of older people in the population, the mortality rates would stop dropping and level out as older people die sooner than younger people.

- b. Interpret the 11.82% for 2010 in slide 2 and compare to the 25% on the vertical axis.

In 2010 11.82% of the population was in the 55 – 64 age bracket, and 25% of the population was 55 and older.

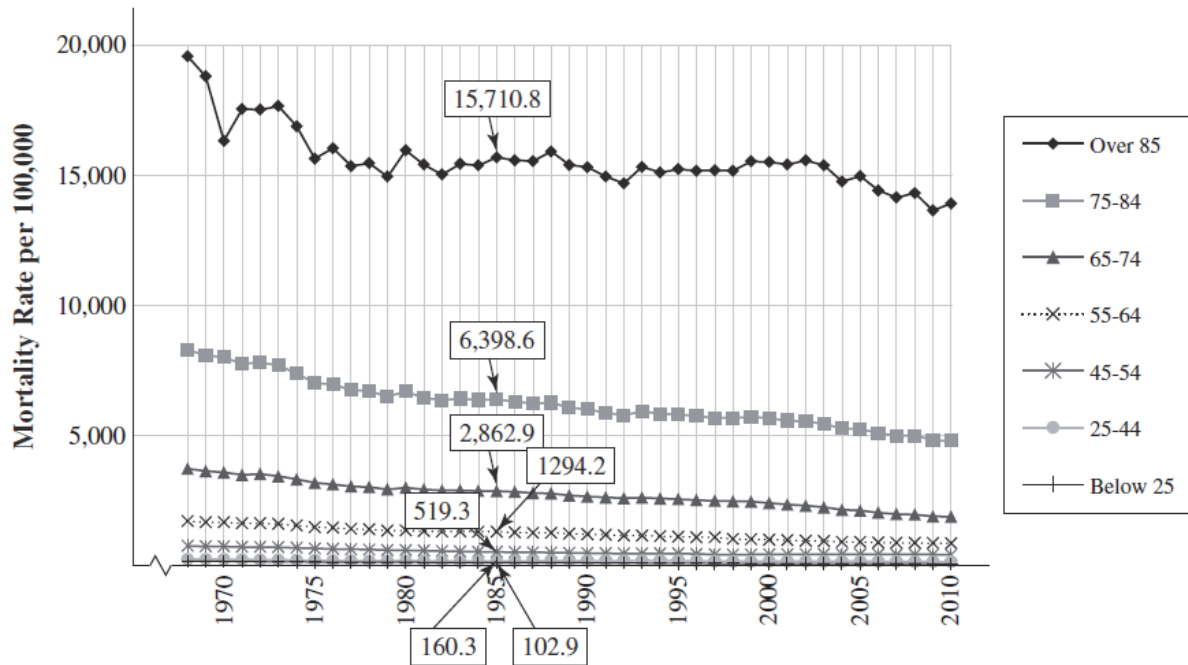
4. Looking at the graph below, which line stands out from the rest? What do you think accounts for this difference?



Data from: <http://www.bloomberg.com/dataview/2014-04-17/how-americans-die.html>

The 25–44 mortality rate line shoots up in the mid-1990's. This was due to AIDS:

5. Interpret the statistics 80.16 and 64.03 for 1985 on graph in #4. Hint: Compare to the statistics shown here, and note that **in 1968** the mortality rate for over 85 was 19,598.5 per 100,000 and the rate for below 25 was 160.7 per 100,000.



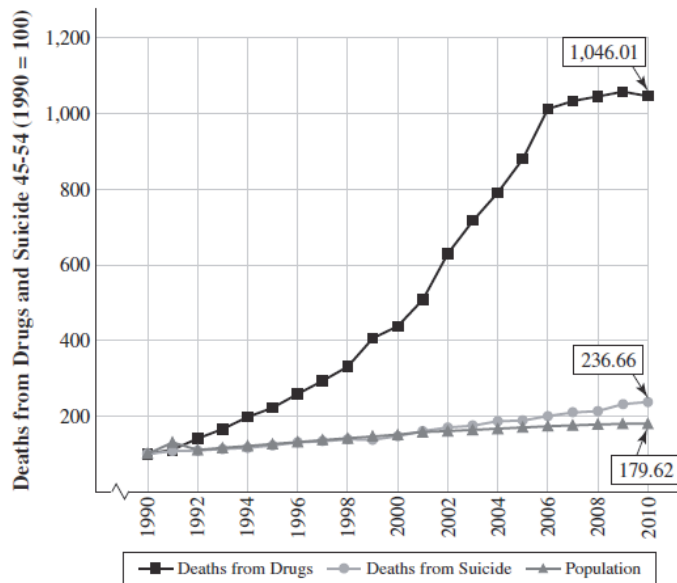
Data from: <http://www.bloomberg.com/dataview/2014-04-17/how-americans-die.html>

Looking at the 1985 statistics above in #5 we see a mortality rate of 15,710.8 deaths per 100,000 for over 85, and 102.9 deaths per 100,000 for under 25. The graph in #4 has set the rates for 1968 (19,598.5 and 160.7 respectively) equal to 100. The 80.16 in #4 comes from the proportion:

$$\frac{15,710.8}{19,598.5} = \frac{x}{100}$$

Telling us that the rate for the over 85 group in 1985 is 80.16% of the 1968 rate. Similarly the rate for the under 25 group in 1985 is 64.03% of the 1968 rate.

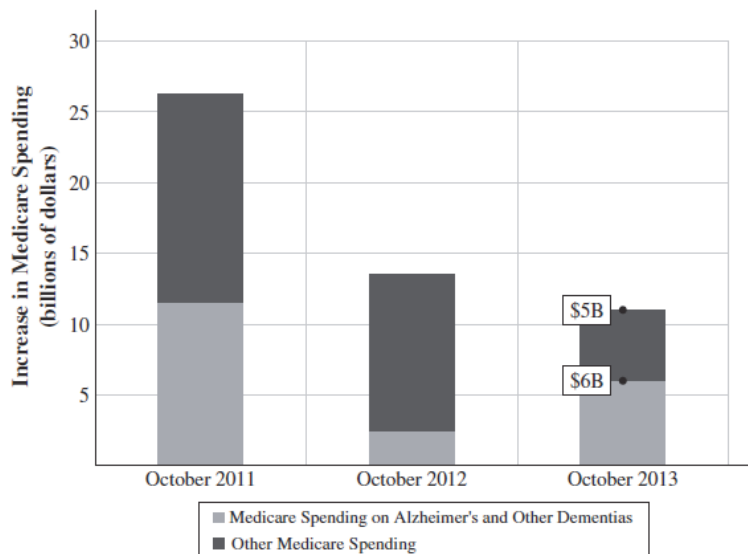
6. Deaths from drugs in the 45 to 54 year old populations have increased by what factor from 1990 to 2010 as shown in this graph? Note the values for 1990 are set to 100.



Data from: <http://www.bloomberg.com/dataview/2014-04-17/how-americans-die.html>

$$\frac{1,046.01}{100} = 10.46 \text{ so a factor of 10.}$$

7. Does this graph indicate Medicare spending has been increasing or decreasing since 2010?



Data from: <http://www.bloomberg.com/dataview/2014-04-17/how-americans-die.html>

Medicare spending has been increasing, the increase has been decreasing. Look at the vertical axis it is "Increase in spending" not "spending"!

Chapter 1 – An Excel-lent Approach to Relationships

Section 1.1 Functions

Objective 1 – Learn Function Basics

Objective 2 – Explore Financial Functions

Objective 1 – Learn Function Basics

Guided Practice Activity #1 – Reasoning About Functions

1. The annual cost of a car is a function of many inputs. List all of the inputs you can think of that determine the output of the annual car cost.

gas, insurance, repairs, etc.

2. Determine which of the following are functions:

INPUTS	OUTPUT	FUNCTION?
States	Senators	No, 2 senators (outputs) per state (input).
Senators	States	Yes, each senator (input) has 1 and only 1 state (output).
States	Number of senators	Yes, constant function each state (input) has same output (2).
People	Anyone they been married to...	No, the output will be multiple people for some inputs.
People	Number of spouses	Yes, the output is a single number for each person.
US Citizens	Social Security Numbers	Yes, one-to-one function.
SS#'s	US Citizens	Yes, one-to-one function.
People	Birthdays	Yes
Birthdays	People born on that day	No
Students in this class	Shoe size	Yes
Shoe Size	Students in this class with that shoe size	No

- Come up with a function between two quantities which remains a function when you switch the inputs and outputs...

Input: Number of gallons of water

Output: Weight of the water

Excel Preview – 1.1 Heart Rate

	A	B	C	D	E	F	G
1							
2							
3							
4							
5							
6							
7		a.)					
8		Input Age:	18				
9		Output Heart Rate:	141.4				
10							
11							

Average heart rate (in beats per minute) is given by the following formula:
Heart Rate = (220 – Age) * 70%.

a.) Enter a formula in the cell C9 of Age (years). Be sure to use the correct formula for an 18 year old v

- What formula would you type into cell C9?

$= (220 - C8) * 70\%$

- According to this formula heart rate is a function of what input?

age

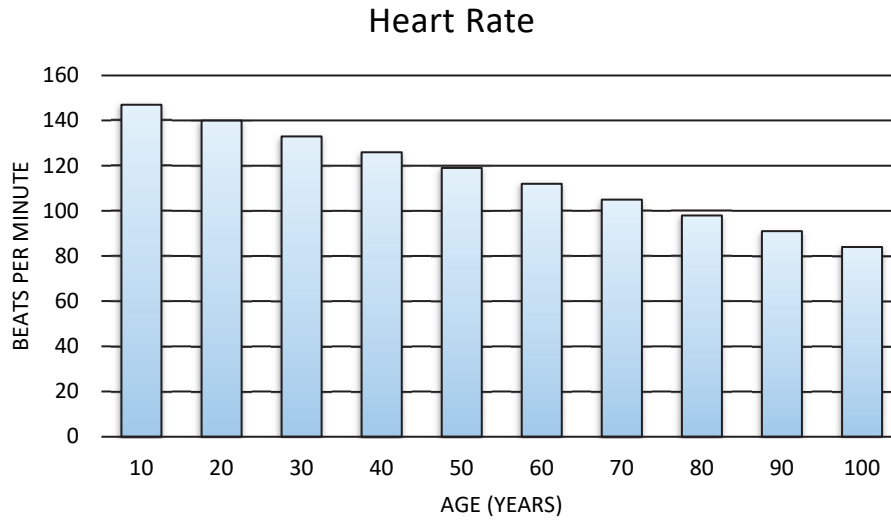
- What are the units for the inputs and outputs for this function?

age: years

heart rate: BPM (beats per minute)

4. To make the following column chart how to we get the category x-axis labels to appear?

use Select Data and highlight the ages



Objective 2 – Explore Financial Functions

Guided Practice Activity #2 – Periodic Rates

For each of the following situations determine the periodic rate (four decimal places of accuracy), and the amount of interest charged in the first period. Creating a spreadsheet to do this will greatly speed up your work!

1. Balance = \$576 APR = 8% weekly
 - a. Weekly rate?
0.1538%
 - b. First week's interest?
\$0.89
2. Balance = \$1396 APR = 3.5% daily
 - a. Daily rate?
0.0096%
 - b. First day's interest?
\$0.13
3. Balance = \$18,500 APR = 14% monthly
 - a. Monthly rate?
1.1667%
 - b. First month's interest?
\$215.83
4. Balance = \$18,500 APR = 1% monthly
 - a. Monthly rate?
0.0833%
 - b. First month's interest?
\$15.42
5. Balance = \$450 APR = 240% monthly
 - a. Monthly rate?
20%

- b. First month's interest?

\$90.00

Guided Practice Activity #3 – Financial Literacy: Credit Card Loan

Let us assume you buy a Sony flat screen TV for your dorm room that costs \$1,000. You make the purchase with a store credit card that has a 12% *Annual Percentage Rate* (APR). You do not have to make any monthly payments for the first year (sounds good!), but they will charge interest at the end of each month. How much do you owe at the end of the first year?

1. What is the Principal?

\$1,000

2. What is the monthly (periodic) interest rate?

1%

3. Monthly interest is a function of what two inputs?

APR and Balance

4. What is the interest charged for the first month?

\$10

Double-click on the fill handle of the highlighted cells to quickly fill down to month 12 (you must have months 1-12 already filled in).

B5								
	A	B	C	D	E	F	G	H
1	Buying a Flat Screen TV					Principal:	\$ 1,000.00	
2						APR:	12%	
3	Month	Balance	Interest	New Balance		Period:	Month	
4	1	\$ 1,000.00	\$ 10.00	\$ 1,010.00		No. of periods		
5	2	\$ 1,010.00	\$ 10.10	\$ 1,020.10		in 1 year:	12	
6	3					Periodic Rate:	1.0%	
7	4							

Cell Reference Handbook

<i>Relative</i>	A4	Changes the row number when you fill up/down and changes the column letter when you fill left/right.
<i>Mixed</i>	SA4	Changes the row number when you fill up/down and fixes the column letter when you fill left/right.
<i>Mixed</i>	A\$4	Fixes the row number when you fill up/down and changes the column letter when you fill left/right.
<i>Absolute</i>	SA\$4	Fixes the row number when you fill up/down and fixes the column letter when you fill left/right.

5. In the spreadsheet above, what formula is in cell C4? D4?

=B4*\$G\$6 and =B4+C4

6. Which formula involves an *absolute cell reference*?

=B4*\$G\$6

7. Why do we need to fill in the second row before we fill the formulas down?

To link the beginning of month 2 to the end of Month 1, which are the same value.

8. What do you owe at the end of the first year?

\$1,126.83

9. What is the APY?

12.683%

Excel Preview – 1.3 TV Loan

	A	B	C	D	E	F	G	H
1	Buying a Flat Screen TV						Principal:	\$1,000.00
2		Part a:					APR:	12%
3	Month	Balance	Interest	Payment	New Balance		Period:	Month
4	1	\$1,000.00	\$ 10.00	\$ 50.00			No. of periods	
5	2						in 1 year:	12
6	3						Periodic Rate:	1.0%
7	4							
8	5							

- Assuming we now make a \$50 payment, what formula is entered into cell **E4**?

=B4 + C4 – D4

- What will the balance be at the start of month 2?

\$960

- What formula is entered in cell **B5**?

=E4

- What formulas are entered in cells **C5**, **D5**, and **E5**?

=H\$6*B5

=D4

=B5 + C5 – D5

- Why do we need to fill in the formulas for month 2 before filling all of them down?

Need to connect beginning of month to end of previous month

- Can we fill down all the formulas for month 2 together? How?

Yes! Highlight the entire row, grab the fill handle and pull down.

Section 1.2 Analytic Representatives: Equations

Objective 1 – Understand Order of Operations

Objective 2 – Evaluate Payment Function

Objective 1 – Understand Order of Operations

Guided Practice Activity #4 – Order of Operations

1. For each of the following compute using proper order of operations without a calculator.

a. $2 - 8/4 + 6 * 2$

12

b. $3^2 + 1$

10

c. $60/(2+8) - 2^3 * 2$

-10

d. $5 + 5/5 + 5$

11

e. $12/6 * 4$

8

2. Write down how you would type these into Excel as a formula:

a. $\frac{2+4}{3*6} - 6$

=(2+4)/(3*6)-6

b. $5 + \frac{2}{(8*4)^{3+1}}$

=5+2/(8*4)^(3+1)

c. $\left(\frac{9+2}{8-11}\right)^{4*6} - 1$

=((9+2)/(8-11))^(4*6)-1

Excel Preview – 1.5 Taxes

	A	B	C	D	E	F	G	H	I	J	K
1	The table below for computing 2018 federal income tax (using new 2017 tax law) in the married filing jointly bracket can be found at:							a.)	b.)	c.)	d.)
2	https://fa.morganstanley.com/balog/mediahandler/media/117520/2018_Tax_Tables.pdf						Income	Base Tax	Amt Over	Rate	TAX
3							\$123,000				
4											
5	If Taxpayer's Income Is...			Then Estimated Taxes Are...							
6	Between	But Not Over	Base Tax	+ Rate	Of the Amount Over						
7	\$0	\$19,050	\$0	10%	\$0						
8	\$19,050	\$77,400	\$1,905.00	12%	\$19,050						
9	\$77,400	\$165,000	\$8,907.00	22%	\$77,400						
10	\$165,000	\$315,000	\$28,179.00	24%	\$165,000						
11	\$315,000	\$400,000	\$64,179.00	32%	\$315,000						
12	\$400,000	\$600,000	\$91,379.00	35%	\$400,000						
13	\$600,000	-----	\$161,379.00	37%	\$600,000			e.)			
14							Income	Base Tax	Amt Over	Rate	Tax
15							\$ 78,000.00				
16							\$ 79,000.00				
17							\$ 80,000.00				
18							\$ 81,000.00				

- For a married couple filing jointly who make \$123,000 in 2018 what is their base tax?

\$8,907.00

- How much more do they make than the “Of the Amount Over” value from column E for their row in the table?

\$45,600

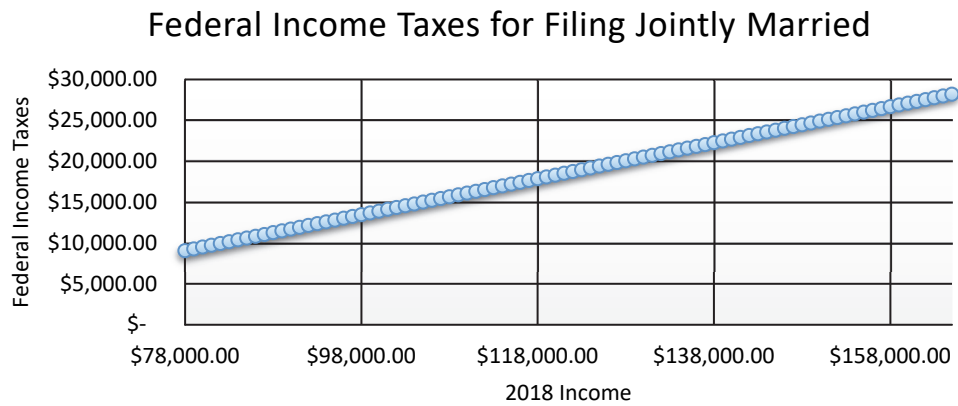
- Compute their estimated taxes by adding the base tax and the correct percentage of the amount they make over the cutoff value. Note there is no division here! The word “over” implies “more than”.

\$18,939

- Are you surprised by how much they pay in taxes?

5. To make the following scatterplot chart what columns have been highlighted?

G and K



Objective 2 – Evaluate Payment Function

Guided Practice Activity #5 – Payment Formula Using Order of Operations

You have just bought a new VW Jetta for \$17,254.38. You put down \$2,254.38 of your savings so you only have to borrow \$15,000. The auto dealership gets you a loan from a bank for 5 years at 6%, which you agree to and sign. What will be your fixed monthly payment?

The periodic payment is a function of 4 inputs:

INPUTS	OUTPUT
Principal (P)	Periodic payment (PMT)
APR	
Number of periods in 1 year (n)	
Number of years of the loan (t)	

$$PMT = \frac{P \times \frac{APR}{n}}{\left(1 - \left(1 + \frac{APR}{n}\right)^{-nt}\right)}$$

Use the following spreadsheet to answer the questions:

	A	B	C	D	E
1	P	APR	n	t	PMT
2	\$ 15,000.00	6%	12	5	\$ 289.99
3					

1. What is the term for this loan?

5 years

2. How many total payments will be made?

60

3. What will be the total amount paid?

\$17,399.40

4. What is the total amount interest paid?

\$2,399.40

5. What formula is entered in cell E2? Does APR/n need its own parentheses?

$$=(A2*B2/C2)/(1-(1+B2/C2)^{(-C2*D2)})$$
 NO!

Excel Preview – 1.6 BMI

	A	B	C	D	E	F	G	H
1								
2								
3								
4								
5								
6								
7								
8								
9								
10								
11								

Input Height:

Feet:

Inches: a.)

Convert Height to Inches:

Input Weight:

Pounds: b.)

Compute Body Mass Index (BMI):

$$BMI = \frac{\text{Weight (lbs)} * 0.45}{(\text{Height (in.)} * 0.025)^2}$$

1. What formula is typed into F6?

$$=C4*12 + C5$$

2. Are parentheses needed in this formula?

No

3. What formula is typed into cell F9?

$$=C8*0.45/(F6*0.025)^2$$

4. BMI is an index number and is meaningless without context. What else do we need to know in order to make sense out of the BMI computed in F9?

Range of values for possible BMI, with some sense of low and obese.

Section 1.3 Numerical and Graphical Representations: Tables and Charts

Objective 1 – Use Multiple Inputs to Understand What-If Analysis

Objective 2 – Convert Tables to Effective Graphs

Objective 1 – Use Multiple Inputs to Understand What-If Analysis

Guided Practice Activity #6 – Monthly Car Payments as Function of Two Inputs

You have just bought a new VW Jetta for \$17,254.38. You put down \$2,254.38 of your savings so you only have to borrow \$15,000. The auto dealership gets you a loan from a bank for 5 years at 6%, which you agree to and sign. What will be your fixed monthly payment?

The periodic payment is a function of 4 inputs:

INPUTS	OUTPUT
Principal (P)	Periodic payment (PMT)
APR	
Number of periods in 1 year (n)	
Number of years of the loan (t)	

$$PMT = \frac{P \times \frac{APR}{n}}{\left(1 - \left(1 + \frac{APR}{n}\right)^{-nt}\right)}$$

In the following spreadsheet we have already explored cell **E2** that is a function of the four inputs in cells **A2:D2**. Now we will consider the two-way table in **B6:H16**, where we are holding the principal, $P = \$15,000$, fixed along with the number of months in one year, $n = 12$. The monthly car payment becomes a function of two inputs: APR and term.

	A	B	C	D	E	F	G	H
1	P	APR	n	t	PMT			
2	\$ 15,000.00	6%	12	5	\$ 289.99			
3								
4		Table Showing Monthly Payments for Different APRs and Terms						
5		Term: Number of Years (t)						
6			1	2	3	4	5	6
7	APR	1%	\$ 1,256.78	\$ 631.53	\$ 423.12	\$ 318.92	\$ 256.41	\$ 214.73
8		2%	\$ 1,263.58	\$ 638.10	\$ 429.64	\$ 325.43	\$ 262.92	\$ 221.26
9		3%	\$ 1,270.41	\$ 644.72	\$ 436.22	\$ 332.01	\$ 269.53	\$ 227.91
10		4%	\$ 1,277.25	\$ 651.37	\$ 442.86	\$ 338.69	\$ 276.25	\$ 234.68
11		5%	\$ 1,284.11	\$ 658.07	\$ 449.56	\$ 345.44	\$ 283.07	\$ 241.57
12		6%	\$ 1,291.00	\$ 664.81	\$ 456.33	\$ 352.28	\$ 289.99	\$ 248.59
13		7%	\$ 1,297.90	\$ 671.59	\$ 463.16	\$ 359.19	\$ 297.02	\$ 255.74
14		8%	\$ 1,304.83	\$ 678.41	\$ 470.05	\$ 366.19	\$ 304.15	\$ 263.00
15		9%	\$ 1,311.77	\$ 685.27	\$ 477.00	\$ 373.28	\$ 311.38	\$ 270.38
16		10%	\$ 1,318.74	\$ 692.17	\$ 484.01	\$ 380.44	\$ 318.71	\$ 277.89
17								

1. What are the two specific inputs, APR and term, for the highlighted payment of \$456.33?

6% and 3 years

2. What formula is entered in cell C7 that will allow us to fill down and across? Note you may use the number 12 in your formula instead of the cell reference C2 since this is constant for monthly payments. In particular pay attention to what cell references are absolute, relative and mixed.

$$= (\$A\$2 * \$B7 / 12) / (1 - (1 + \$B7 / 12)^{-12 * C\$6})$$

3. How much total interest is paid with the \$289.99 monthly payment?

$$\$2,399.40 = 5 * 12 * \$289.99 - \$15,000$$
 Note using values from spreadsheet gives slightly different answer: \$2,399.52

4. How much would you save in interest if you switched your 5 year 6% loan to 3 years at 6%?

$$\$971.52 = \$2,399.40 - (3 * 12 * \$456.33 - \$15,000)$$

5. What if you have a horrible credit score you might be forced to take out a 6 year loan at 10%. How much interest do you pay over the life of this loan?

$$\$5,008.08 = 6 * 12 * \$277.89 - \$15,000$$

6. What is fixed (column or row) by the following cell references?

\$F\$4	G\$2	T1	\$V85	J\$21	\$S99
Both	Row	Neither	Both	Row	Column

Objective 2 – Convert Tables to Effective Graphs

Guided Practice Activity #7 – Effective Charts of Two Way Tables

To make an effective chart of a two way table we often simply highlight one column of data and then add appropriate labels. Let's assume we want to make a chart showing the monthly payments a 5 year loan of \$15,000 as a function of the different APR's.

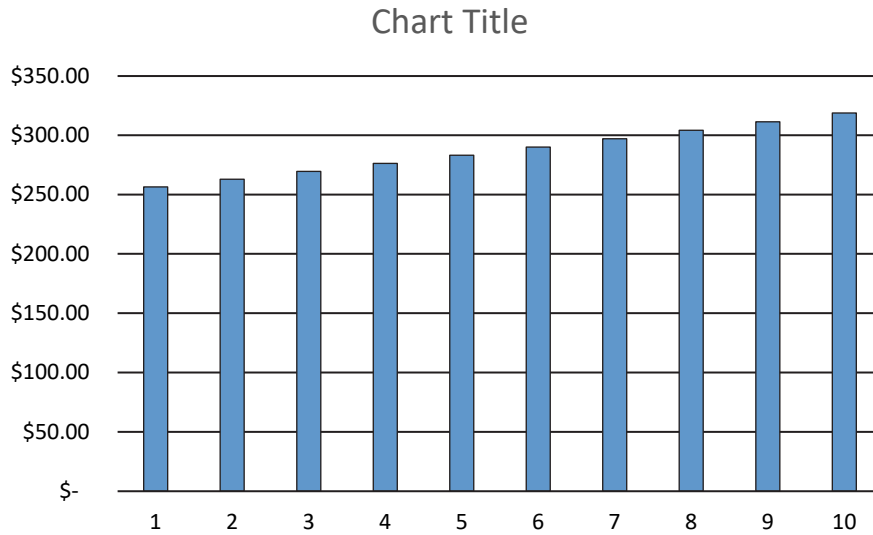
	A	B	C	D	E	F	G	H
1	P	APR	n	t	PMT			
2	\$ 15,000.00	6%	12	5	\$ 289.99			
3								
4		Table Showing Monthly Payments for Different APRs and Terms						
5		Term: Number of Years (t)						
6			1	2	3	4	5	6
7	APR	1%	\$ 1,256.78	\$ 631.53	\$ 423.12	\$ 318.92	\$ 256.41	\$ 214.73
8		2%	\$ 1,263.58	\$ 638.10	\$ 429.64	\$ 325.43	\$ 262.92	\$ 221.26
9		3%	\$ 1,270.41	\$ 644.72	\$ 436.22	\$ 332.01	\$ 269.53	\$ 227.91
10		4%	\$ 1,277.25	\$ 651.37	\$ 442.86	\$ 338.69	\$ 276.25	\$ 234.68
11		5%	\$ 1,284.11	\$ 658.07	\$ 449.56	\$ 345.44	\$ 283.07	\$ 241.57
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16		10%	\$ 1,318.74	\$ 692.17	\$ 484.01	\$ 380.44	\$ 318.71	\$ 277.89
17								

1. What cell range should you highlight for this chart?

G7:G16

2. The following chart does not have correct x-axis labels. How do you get the APR's to show up on the x-axis?

Click on Select Data and then edit Horizontal Category Axis Labels by selecting cells B7:B16.



3. How do you add axis titles and the chart title?

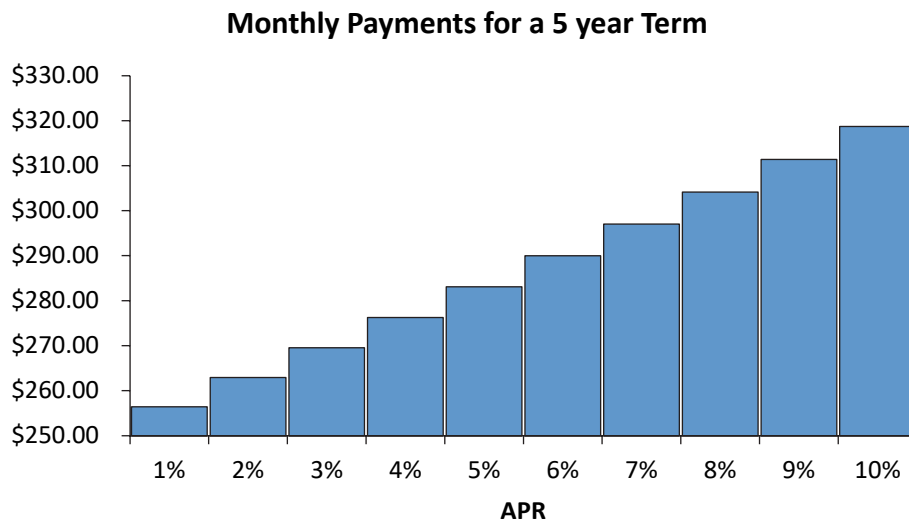
Add Chart Element

4. How do you make the columns wider?

Right click on a column and choose Format Data Series and set gap Width to 5% or so

5. How do you make the vertical axis start at \$250 to accentuate the difference in monthly payments?

Right click on vertical axis number and select Format Axis, set Minimum to 250



Excel Preview – 1.10 Wind Chill

The following screenshot gives the formula for Wind Chill.

	A	B	C	D	E	F	G	H	I	J	K	L	M
1				Wind chill is a function of the outside temperature (°F) and the wind speed (mph): Wind Chill(°F) = $35.74 + 0.6215 * \text{Temp}(°F) - 35.75 * \text{Speed}(\text{mph})^{0.16} + 0.4275 * \text{Temp}(°F) * \text{Speed}(\text{mph})^{0.16}$.									
2													
3													
4			a.)										
5	Temperature (°F)		13	a.) Enter a formula that outputs the Wind Chill given the inputs of Temperature and Wind Spe									
6	Wind Speed (mph)		9										
7	Wind Chill (°F)		0.9										
8													
9													
10			b.)										
11			Note: Formula does not work for a wind speed of zero.										
12			Temp (°F)	Wind Speed (mph)									
13				1	3	5	7	9	11	13	15	17	19
14			-15	-15.7	-23.8	-28.1	-31.1	-33.5	-35.5	-37.1	-38.6	-39.9	-41.1
15			-11	-11.5	-19.3	-23.4	-26.3	-28.6	-30.5	-32.1	-33.5	-34.7	-35.9
16			-7	-7.4	-14.8	-18.7	-21.5	-23.7	-25.5	-27.0	-28.4	-29.6	-30.7
17			-3	-3.2	-10.3	-14.0	-16.7	-18.8	-20.5	-21.9	-23.2	-24.4	-25.4
18			1	1.0	-5.7	-9.3	-11.9	-13.8	-15.5	-16.9	-18.1	-19.2	-20.2
19			5	5.2	-1.2	-4.6	-7.0	-8.9	-10.5	-11.8	-13.0	-14.0	-15.0
20			9	9.4	3.3	0.1	-2.2	-4.0	-5.5	-6.8	-7.9	-8.9	-9.8
21			13	13.6	7.8	4.8	2.6	0.9	-0.5	-1.7	-2.7	-3.7	-4.5
22			17	17.8	12.3	9.5	7.4	5.8	4.5	3.4	2.4	1.5	0.7
23			21	22.0	16.9	14.2	12.2	10.7	9.5	8.4	7.5	6.7	5.9

1. In cell D14 what are the inputs for the output of -15.7 degrees?

-15 degrees and 1 mph

2. What formula is in cell D14 that you can fill down and across? Pay attention to what should be a relative versus absolute or mixed cell reference.

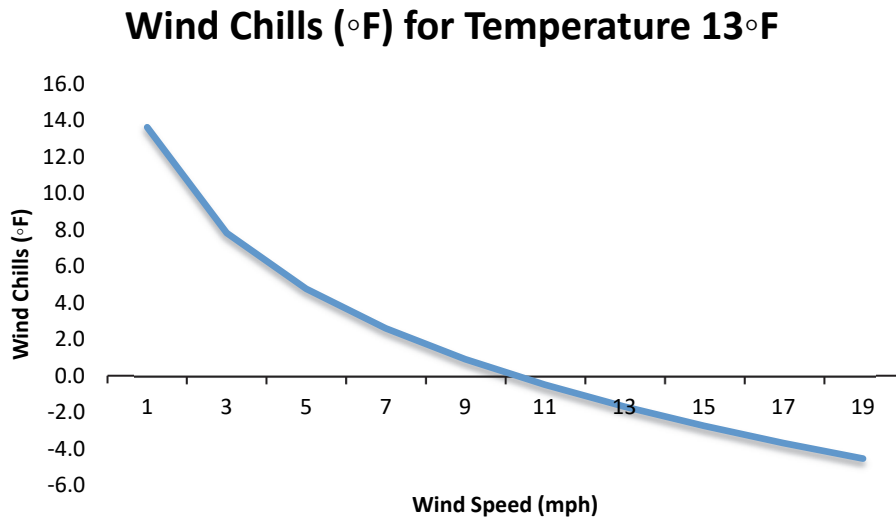
Wind Chill(°F) =

$$35.74 + 0.6215 * \text{Temp}(°F) - 35.75 * \text{Speed}(\text{mph})^{0.16} + 0.4275 * \text{Temp}(°F) * \text{Speed}(\text{mph})^{0.16}$$

$$=35.74 + 0.6215 * \$C14 - 35.75 * D\$13^{0.16} + 0.4275 * \$C14 * D\$13^{0.16}$$

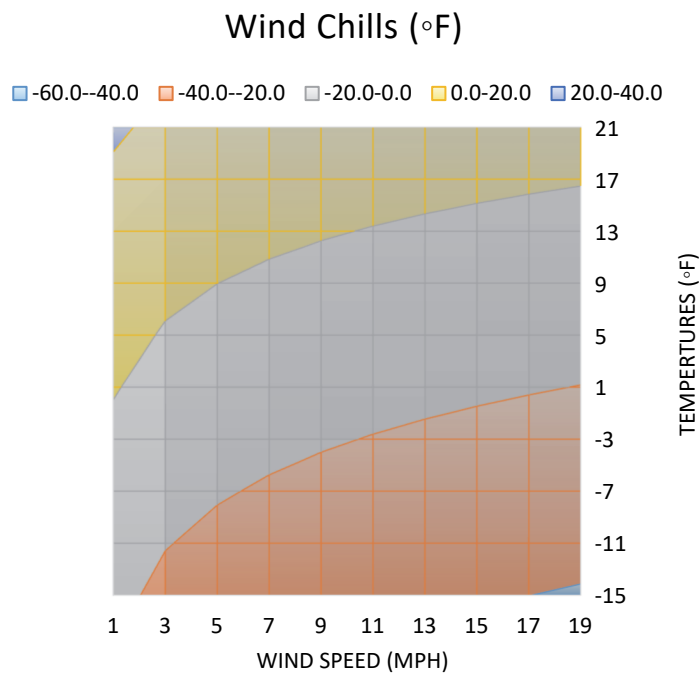
3. What cell range was highlighted to make the following line chart?

D21:M21



4. What cell range was highlighted to make the following surface chart?

C13:M23



Excel Preview – 1.6 BMI

BMI is calculated using the formula:

$$\text{BMI} = \frac{\text{Weight (lbs)} * 0.45}{(\text{Height (in.)} * 0.025)^2}$$

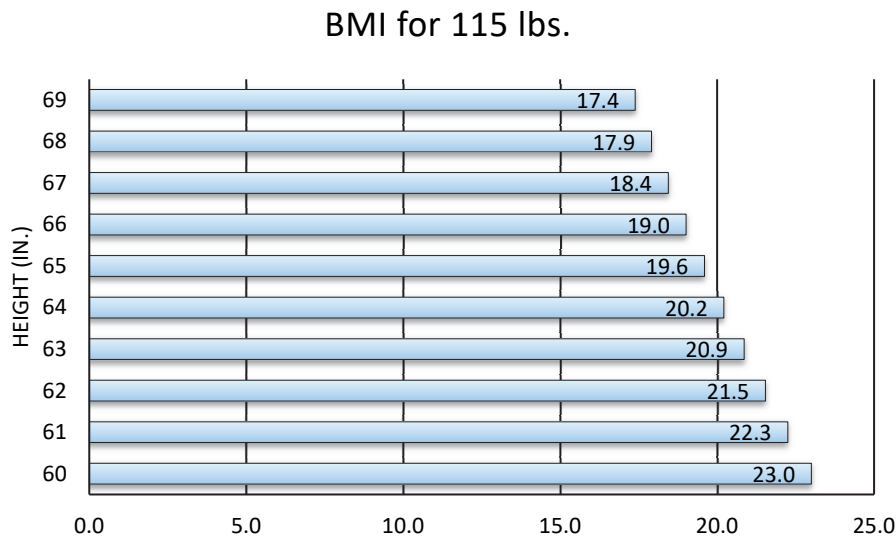
20		c.)										
21			C	D	E	F	G	H	I	J	K	L
22		Height (in)	Weight (lbs)									
23			105	110	115	120	125	130	135	140	145	150
24		60	21.0	22.0	23.0	24.0	25.0	26.0	27.0	28.0	29.0	30.0
25		61	20.3	21.3	22.3	23.2	24.2	25.2	26.1	27.1	28.1	29.0
26		62	19.7	20.6	21.5	22.5	23.4	24.3	25.3	26.2	27.2	28.1
27		63	19.0	20.0	20.9	21.8	22.7	23.6	24.5	25.4	26.3	27.2
28		64	18.5	19.3	20.2	21.1	22.0	22.9	23.7	24.6	25.5	26.4
29		65	17.9	18.7	19.6	20.4	21.3	22.2	23.0	23.9	24.7	25.6
30		66	17.4	18.2	19.0	19.8	20.7	21.5	22.3	23.1	24.0	24.8
31		67	16.8	17.6	18.4	19.2	20.0	20.9	21.7	22.5	23.3	24.1
32		68	16.3	17.1	17.9	18.7	19.5	20.2	21.0	21.8	22.6	23.4
33		69	15.9	16.6	17.4	18.1	18.9	19.7	20.4	21.2	21.9	22.7
34												

1. What formula would you type into cell **C24** that can be filled down and across?

=C\$23*0.45/(\$B24*0.025)^2

2. What cell range would be highlighted to make the following chart?

E24:E33



Section 1.4 Spotlight on Statistics

Objective 1 – Learn Descriptive Statistics
Objective 2 – Compute Weighted Averages
Objective 3 – Create Histograms

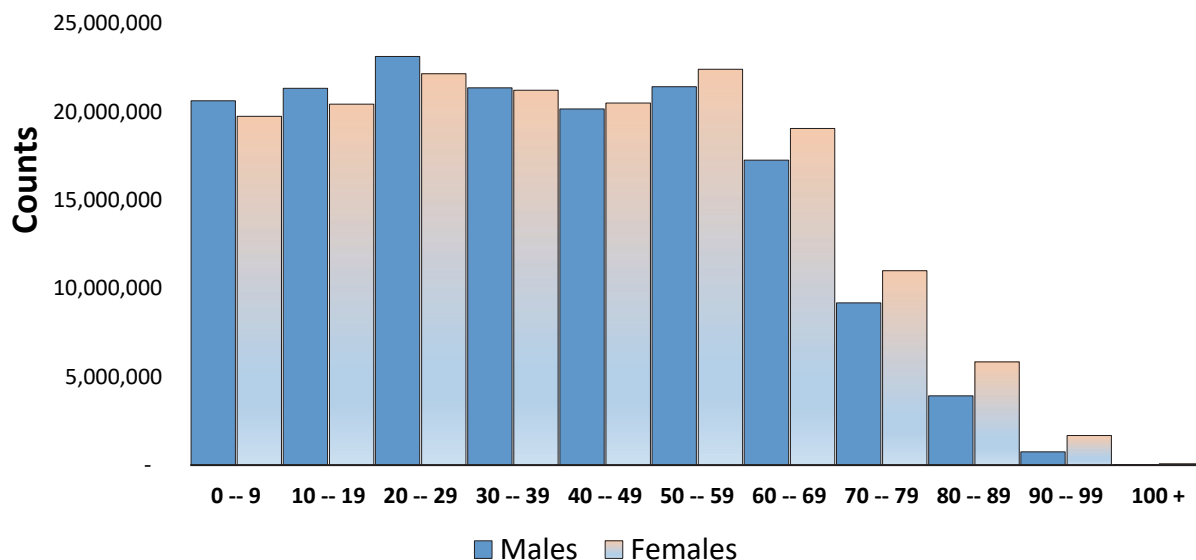
Objective 1 – Learn Descriptive Statistics

Guided Practice Activity #8 – Age Distribution

The table and chart give the distribution of ages in the U.S. in 2016.

Bins	Males	Females
0 -- 9	20,616,776	19,740,060
10 -- 19	21,320,578	20,427,654
20 -- 29	23,122,539	22,149,373
30 -- 39	21,344,706	21,215,558
40 -- 49	20,152,276	20,491,598
50 -- 59	21,413,590	22,405,574
60 -- 69	17,252,551	19,050,568
70 -- 79	9,177,809	11,000,333
80 -- 89	3,916,541	5,834,320
90 -- 99	745,215	1,667,998
100 +	16,342	65,554

U.S. Age Distribution 2016



1. What are the heights of the columns for the first bin in which women outnumber men? What do these heights represent?

20,152,276 men and 20,491,598 in the 40–49 year old age range

2. The text indicates the median age is about 38 years old. What does this mean?

Half the population is younger than 38 and half older

3. Compute the number of people from 0 – 39 and 40 and above. Are these close to being equal?

169,937,244 under 40 and 153,190,269 over, yes close!