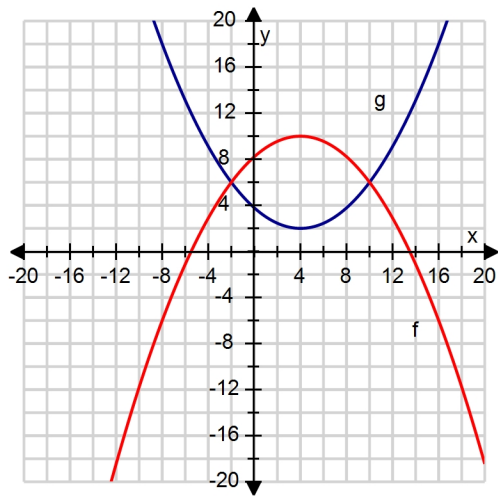


Test Bank for Biocalculus - Calculus Probability and Statistics for the Life Sciences 2nd Stewart

1.1 Four Ways to Represent a Function

1. The graphs of $f(x)$ and $g(x)$ are given. For what values of x is $f(x) = g(x)$?



- a. 2, 3
- b. 0
- c. -1
- d. -2, 5
- e. -2, 10

ANSWER: e

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.4b SCalc7e 1.1.4b

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.CO.H.LO.01.01.12 - Express a function numerically, given its verbal, algebraic, or graphical representation.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 2/24/2020 9:14 AM

1.1 Four Ways to Represent a Function

2. Which of the following functions is neither even nor odd?

a. $f(x) = \frac{2x^2}{x^4 + 1}$

b. $f(x) = 8x^3 + 10x^2 + 7$

c. $f(x) = x^3 - 3x$

ANSWER: b

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.78 SCalc7e 1.1.78

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.04.03 - Determine if a function is odd or even algebraically.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/18/2021 10:52 AM

1.1 Four Ways to Represent a Function

3. If the point $(9, 7)$ is on the graph of an even function, what other point must also be on the graph?

- a. $(-9, -7)$
- b. $(9, -7)$
- c. $(0, 0)$
- d. $(-9, 7)$
- e. None of these

ANSWER: d

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.71a SCalc7e 1.1.71a

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.04.05 - Describe the symmetry present in the graph of an even function.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 2:43 AM

1.1 Four Ways to Represent a Function

4. If $f(x) = x^2 - x + 8$, evaluate the difference quotient $\frac{f(a+h) - f(a)}{h}$.

- a. $2a + h - 8$
- b. $2a - 8$
- c. $2a - h - 8$
- d. h
- e. none of these

ANSWER: e

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.28 SCalc7e 1.1.28

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.08 - Evaluate functions for given values of the independent variable.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

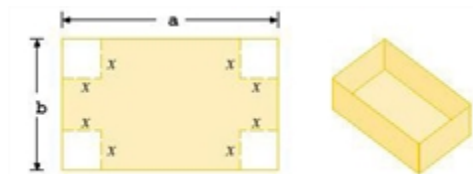
DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 2:48 AM

1.1 Four Ways to Represent a Function

5. A box with an open top is to be constructed from a rectangular piece of card board with dimensions $b = 6$ in. by $a = 25$ in. by cutting out equal squares of side x at each corner and then folding up the sides as in the figure.

Express the volume V of the box as a function of x .



- a. $V(x) = x^3 - 62x^2 + 150x$
- b. $V(x) = 4x^3 + 31x^2 + 196x$
- c. $V(x) = 4x^3 + 62x^2 + 150x$
- d. $V(x) = x^3 - 31x^2 + 196x$
- e. $V(x) = 4x^3 - 62x^2 + 150x$

ANSWER: e

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.63 SCalc7e 1.1.63

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.11 - Express a function algebraically, given its verbal or numerical representation.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 2/10/2020 1:32 AM

1.1 Four Ways to Represent a Function

6. Find an expression for the function $y = f(x)$ whose graph is the bottom half of the parabola $x + (10 - y)^2 = 0$.

a. $y = 10 - \sqrt{-x}$

b. $y = 100 - \sqrt{-x}$

c. $y = 10 + \sqrt{x}$

d. $y = 100 - x^2$

e. $y = 10 - x^2$

ANSWER: a

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.53 SCalc7e 1.1.53

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.11 - Express a function algebraically, given its verbal or numerical representation.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 3:39 AM

1.1 Four Ways to Represent a Function

7. A rectangle has perimeter 14 m. Express the area of the rectangle as a function $A(l)$ of the length l of one of its sides.

a. $A(l) = 7l - l^2$

b. $A(l) = l - 7l^2$

c. $A(l) = 14l - l^2$

d. $A(l) = 14l + l^2$

e. $A(l) = 7l + l^2$

ANSWER: a

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.57 SCalc7e 1.1.57

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.11 - Express a function algebraically, given its verbal or numerical representation.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 3:44 AM

1.1 Four Ways to Represent a Function

8. If $f(x) = 5x^2 + 2$, find and simplify $\frac{f(1+h) - f(1)}{h}$, where $h \neq 0$.

a. $2 + 5h^2$

b. $5 + 10h$

c. $5h$

d. $10 + 5h$

ANSWER: d

POINTS: 1

DIFFICULTY: Easy

REFERENCES: SCalcET7 1.1.27 SCalc7e 1.1.27

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.CO.H.LO.01.01.08 - Evaluate functions for given values of the independent variable.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

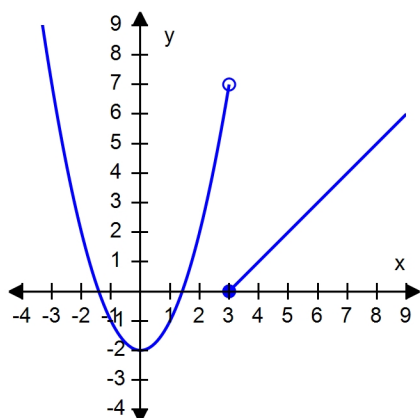
DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 3:59 AM

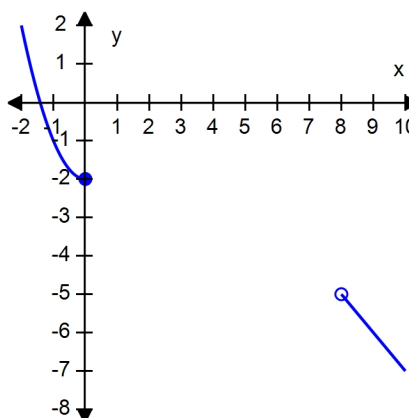
9. Find the domain and sketch the graph of the function. What is its range?

$$f(x) = \begin{cases} -x + 3 & \text{if } x \geq 3 \\ x^2 - 2 & \text{if } x < 3 \end{cases}$$

a. $D: (-\infty, \infty); R: [-2, \infty)$



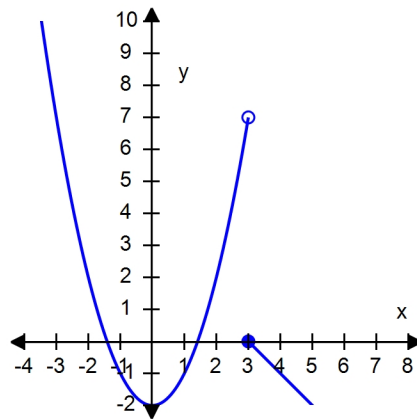
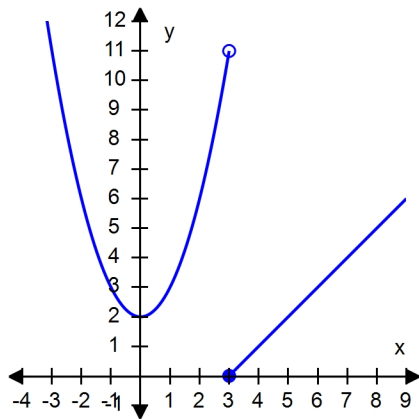
b. $D: (-\infty, \infty); R: (-\infty, 0]$



c. $D: (-\infty, \infty); R: [0, \infty)$

d. $D: (-\infty, \infty); R: (-\infty, \infty)$

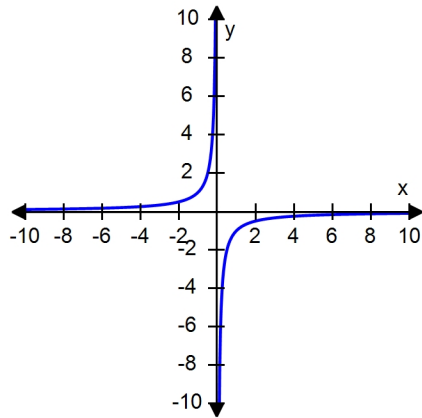
1.1 Four Ways to Represent a Function



ANSWER: d
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.49 SCalc7e 1.1.49
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.01.01.03 - Define range of a function.
OTHER: Bimodal
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 2/25/2020 12:34 AM

1.1 Four Ways to Represent a Function

10. Determine whether the function whose graph is given is even, odd, or neither.

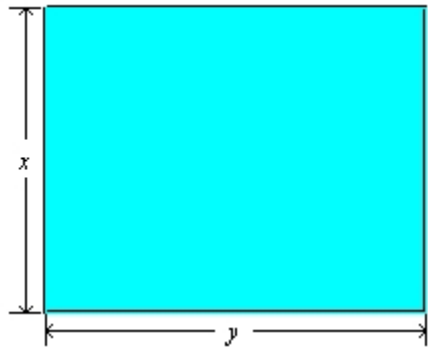


- a. Even
- b. Neither
- c. Odd

ANSWER: c
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.69 SCalc7e 1.1.69
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.01.04.04 - Determine if a function is odd or even graphically.
OTHER: Bimodal
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 2/3/2020 8:06 AM

1.1 Four Ways to Represent a Function

11. Sandy wishes to have a rectangular garden in her backyard. She has 50 ft of fencing with which to enclose her garden. Letting x denote the width of the garden, find a function f in the variable x that gives the area of the garden.



- a. $f(x) = 50x - x^2, 0 < x < 25$
- b. $f(x) = 25x - x^2, 0 < x < 25$
- c. $f(x) = 50x - x^2, 0 < x < 50$
- d. $f(x) = 25x - x^2, 0 < x < 50$

ANSWER: b

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.62 SCalc7e 1.1.62

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.11 - Express a function algebraically, given its verbal or numerical representation.

OTHER: Bimodal

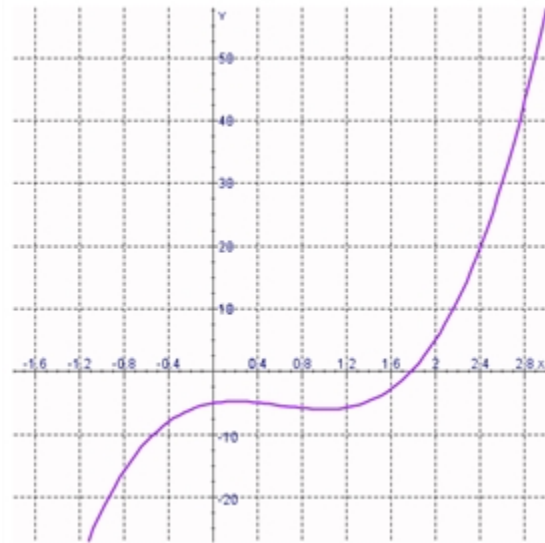
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 2/10/2020 4:17 AM

1.1 Four Ways to Represent a Function

12. The graph of the function f is given. State the value of $f(2.7)$.

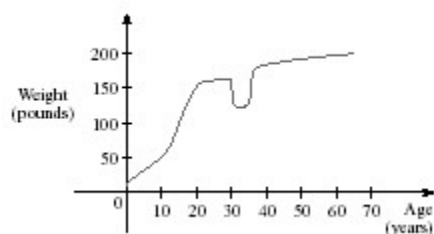


- a. $f(2.7) = -40$
- b. $f(2.7) = -10$
- c. $f(2.7) = 40$
- d. $f(2.7) = 0$
- e. $f(2.7) = 10$

ANSWER: c
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.3b SCalc7e 1.1.3b
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.CO.H.LO.01.02.03 - Identify the value of a function from its graph.
KEYWORDS: 7ET
OTHER: Bimodal
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 2/25/2020 12:37 AM

1.1 Four Ways to Represent a Function

13. The graph shown gives the weight of a certain person as a function of age. Find the age at which the person stopped an exercise program.



- a. 20
- b. 54
- c. 38
- d. 35
- e. 70

ANSWER: d

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.11 SCalc7e 1.1.11

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.12 - Express a function numerically, given its verbal, algebraic, or graphical representation.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 2/25/2020 12:38 AM

1.1 Four Ways to Represent a Function

14. In the function $f(x) = 8x + d$, what must be the value d , if $f(3) = 1$?

- a. $d = 25$
- b. $d = 23$
- c. $d = -23$
- d. $d = -1$
- e. $d = -25$

ANSWER: c

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.25 SCalc7e 1.1.25

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.08 - Evaluate functions for given values of the independent variable.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 5:06 AM

1.1 Four Ways to Represent a Function

15. An open rectangular box with volume 4 m^3 has a square base. Express the surface area of the box as a function $S(x)$ of the length x of a side of the base.

a. $S(x) = x^2 + \frac{16}{x^2}$

b. $S(x) = x^2 + \frac{16}{x}$

c. $S(x) = 2x^2 + \frac{6}{x^2}$

d. $S(x) = x^2 + \frac{6}{x^2}$

e. $S(x) = 2x + \frac{6}{x}$

ANSWER:

b

POINTS:

1

DIFFICULTY:

Medium

REFERENCES:

SCalcET7 1.1.61 SCalc7e 1.1.61

QUESTION TYPE:

Multi-Mode (Multiple choice)

HAS VARIABLES:

True

STUDENT ENTRY MODE:

Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.11 - Express a function algebraically, given its verbal or numerical representation.

KEYWORDS:

7ET

OTHER:

Bimodal

NOTES:

SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED:

7/20/2015 1:44 PM

DATE MODIFIED:

1/29/2020 5:13 AM

1.1 Four Ways to Represent a Function

16. Determine whether f is even, odd, or neither.

$$f(x) = \frac{8x^2}{x^4 + 5}$$

- a. neither
- b. odd
- c. even

ANSWER: c
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.74 SCalc7e 1.1.74
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.01.04.03 - Determine if a function is odd or even algebraically.
OTHER: Bimodal
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 1/29/2020 5:26 AM

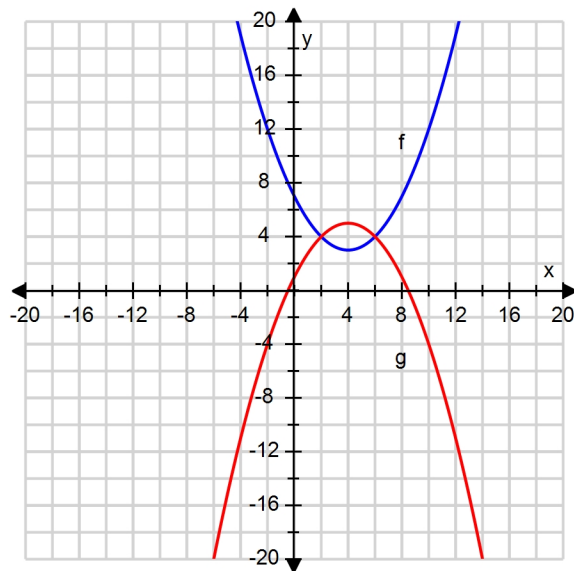
17. Determine whether f is even, odd, or neither.

$$f(x) = \frac{2x^2}{x^4 + 1}$$

ANSWER: even
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.74 SCalc7e 1.1.74
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.04.03 - Determine if a function is odd or even algebraically.
OTHER: Numerical Response
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 1/29/2020 5:42 AM

1.1 Four Ways to Represent a Function

18. The graphs of $f(x)$ and $g(x)$ are given.
- For what values of x is $f(x) = g(x)$?
 - Find the values of $f(-1)$ and $g(12)$.



ANSWER: a) 2, 6 b) $f(-1) = 12$, $g(12) = -10$

POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.4ab SCalc7e 1.1.4ab
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.02.03 - Identify the value of a function from its graph.
OTHER: Numerical Response
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 2/25/2020 5:05 AM

1.1 Four Ways to Represent a Function

19. A spherical balloon with radius r inches has volume $\frac{4}{3} \pi r^3$.

Find a function that represents the amount of air required to inflate the balloon from a radius of r inches to a radius of $r + 7$ inches.

ANSWER: $\frac{28}{3} \pi(3r^2 + 21r + 49)$

POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.26 SCalc7e 1.1.26
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.01.11 - Express a function algebraically, given its verbal or numerical representation.
OTHER: Numerical Response
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 2/10/2020 6:12 AM

1.1 Four Ways to Represent a Function

20. If $f(x) = \begin{cases} x^2 + 7 & \text{if } x \leq 0 \\ \sqrt{x} & \text{if } x > 0 \end{cases}$

find $f(-3)$, $f(0)$, and $f(4)$.

ANSWER: $f(-3) = 16$, $f(0) = 7$, $f(4) = 2$.

POINTS: 1

DIFFICULTY: Easy

REFERENCES: SCalcET7 1.1.25 SCalc7e 1.1.25

QUESTION TYPE: Subjective Short Answer

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.08 - Evaluate functions for given values of the independent variable.

OTHER: Short Answer

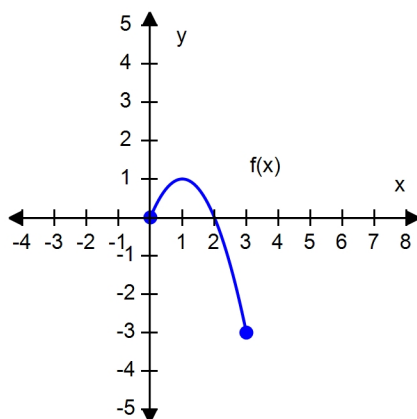
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/30/2020 11:58 PM

1.1 Four Ways to Represent a Function

21. Refer to the graph of the function f in the following figure.



- a. Find $f(0)$.
- b. Find the value of x for which (i) $f(x) = 1$ and (ii) $f(x) = 0$.
- c. Find the domain and range of f .

ANSWER:

- a. 0
- b. (i) 1 (ii) 0, 2
- c. $D: [0, 3]$, $R: [-3, 1]$

POINTS:

1

DIFFICULTY:

Easy

REFERENCES:

SCalcET7 1.1.3ace SCalc7e 1.1.3ace

QUESTION TYPE:

Subjective Short Answer

HAS VARIABLES:

True

STUDENT ENTRY MODE:

Basic

LEARNING OBJECTIVES: PCALC.CO.H.LO.01.01.03 - Define range of a function.

OTHER:

Short Answer

NOTES:

SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED:

7/20/2015 1:44 PM

DATE MODIFIED:

2/7/2020 4:51 AM

1.1 Four Ways to Represent a Function

22. Determine whether the function is even, odd, or neither.

$$f(x) = 4x^2 + 8x + 1$$

ANSWER: Neither

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.77 SCalc7e 1.1.77

QUESTION TYPE: Subjective Short Answer

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.CO.H.LO.01.04.03 - Determine if a function is odd or even algebraically.

OTHER: Short Answer

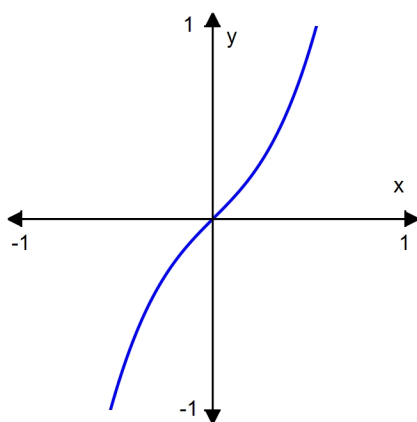
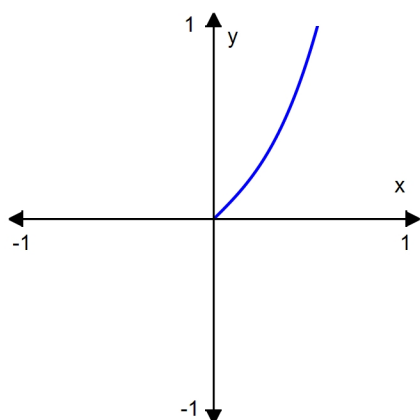
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 6:11 AM

1.1 Four Ways to Represent a Function

23. The following figure shows a portion of the graph of a function f defined on the interval $[-1, 1]$. Sketch the complete graph of f if it is known f is odd.



ANSWER:

POINTS:

1

DIFFICULTY:

Medium

REFERENCES:

SCalcET7 1.1.72b SCalc7e 1.1.72b

QUESTION TYPE:

Subjective Short Answer

HAS VARIABLES:

True

STUDENT ENTRY MODE:

Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.04.09 - Sketch graphs of functions that are symmetric with respect to the x-axis, y-axis, or the origin.

OTHER:

Short Answer

NOTES:

SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED:

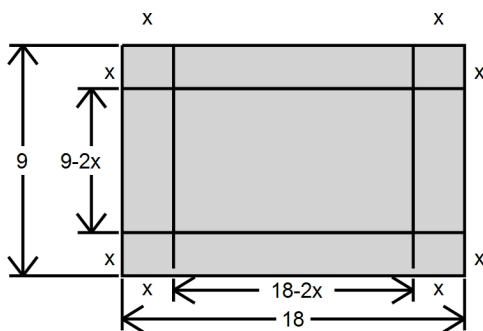
7/20/2015 1:44 PM

DATE MODIFIED:

2/7/2020 4:34 AM

1.1 Four Ways to Represent a Function

24. By cutting away identical squares from each corner of a rectangular piece of cardboard and folding up the resulting flaps, an open box can be made. If the cardboard is 18 in. long and 9 in. wide and the square cutaways have dimensions of x in. by x in., find a function that gives the volume of the resulting box.



ANSWER:

$$V = 4x^3 - 54x^2 + 162x$$

POINTS:

1

DIFFICULTY:

Medium

REFERENCES:

SCalcET7 1.1.63 SCalc7e 1.1.63

QUESTION TYPE:

Subjective Short Answer

HAS VARIABLES:

True

STUDENT ENTRY MODE:

Basic

LEARNING OBJECTIVES: PCALC.CO.H.LO.01.01.11 - Express a function algebraically, given its verbal or numerical representation.

OTHER:

Short Answer

NOTES:

SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED:

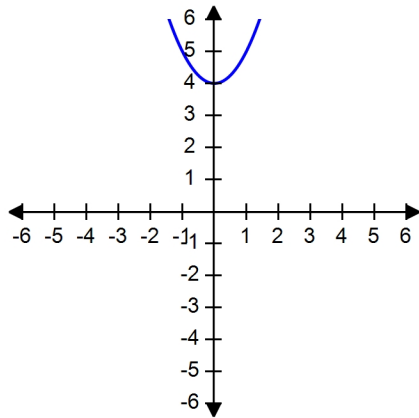
7/20/2015 1:44 PM

DATE MODIFIED:

2/7/2020 4:52 AM

1.1 Four Ways to Represent a Function

25. Use the vertical line test to determine whether the curve is the graph of a function of x .



ANSWER: Yes

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.7 SCalc7e 1.1.7

QUESTION TYPE: Subjective Short Answer

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.06 - Given its graph, determine if a relation is a function using the vertical line test.

OTHER: Short Answer

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

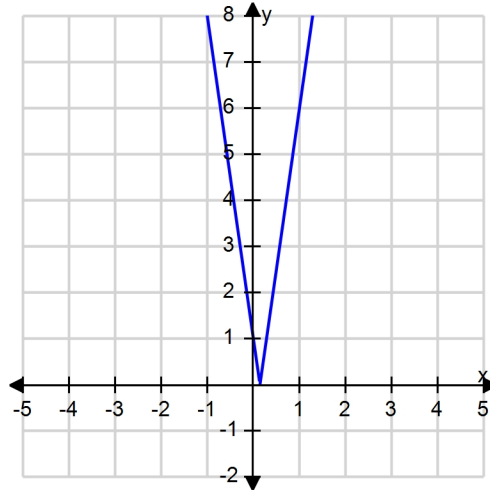
DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 2/7/2020 5:56 AM

1.1 Four Ways to Represent a Function

26. Sketch the graph of the function.

$$f(x) = |1 - 7x|$$



ANSWER:

POINTS: 1

QUESTION TYPE: Subjective Short Answer

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

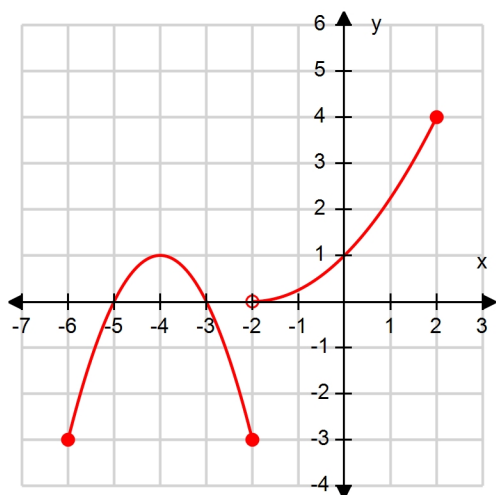
LEARNING OBJECTIVES: PCALC.COH.LO.01.01.13 - Express a function graphically, given its verbal or numerical representation.

DATE CREATED: 1/21/2021 7:28 AM

DATE MODIFIED: 2/5/2021 9:36 AM

1.1 Four Ways to Represent a Function

27. The graph of a function g is given. On what interval(s) is g increasing?



ANSWER: $[-6, -4] \cup (-2, 2]$

POINTS: 1

QUESTION TYPE: Subjective Short Answer

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.02.07 - Find the intervals where a function is increasing and decreasing using its graph.

DATE CREATED: 1/21/2021 7:58 AM

DATE MODIFIED: 2/5/2021 9:36 AM

28. Determine whether the statement is true or false.

If $x_1 > x_2$ and f is a decreasing function, then $f(x_1) > f(x_2)$.

a. True

b. False

ANSWER: False

POINTS: 1

QUESTION TYPE: True / False

HAS VARIABLES: False

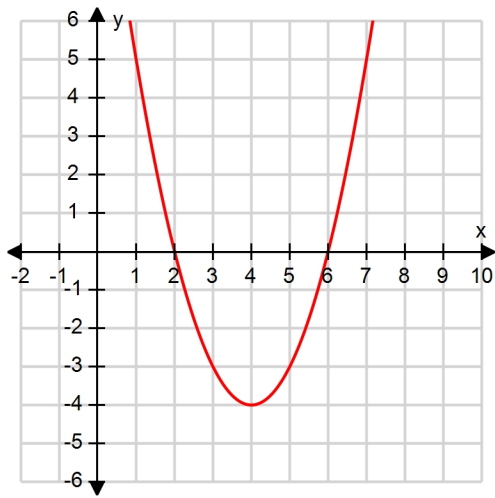
LEARNING OBJECTIVES: PCALC.COH.UO.01.02.02 - Examine the characteristics of functions and their graphs.

DATE CREATED: 1/22/2021 2:50 AM

DATE MODIFIED: 2/5/2021 9:37 AM

1.1 Four Ways to Represent a Function

29. Let f be the function whose graph is given. Find the interval where the function is decreasing.



- a. $(-\infty, 4)$
- b. $(4, \infty)$
- c. $[2, 6]$
- d. $(-4, \infty)$

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.01.02.07 - Find the intervals where a function is increasing and decreasing using its graph.

DATE CREATED: 1/22/2021 3:52 AM

DATE MODIFIED: 2/5/2021 9:37 AM

1.2 A Catalog of Essential Functions

1. Many physical quantities are connected by *inverse square laws*, that is, by power functions of the form:

$$f(x) = kx^{-2}$$

In particular, the illumination of an object by a light source is inversely proportional to the square of the distance from the source. Suppose that after dark you are in a room with just one lamp and you are trying to read a book.

The light is too dim and so you move $\frac{2}{3}$ ds the distance to the lamp. How much brighter is the light?

a. $\frac{3}{2}$ times

b. $\frac{9}{4}$ times

c. $\frac{9}{2}$ times

d. $\frac{4}{9}$ times

e. 3 times

ANSWER:

b

POINTS:

1

DIFFICULTY:

Medium

REFERENCES:

SCalcET7 1.2.25 SCalc7e 1.2.25

QUESTION TYPE:

Multi-Mode (Multiple choice)

HAS VARIABLES:

True

STUDENT ENTRY MODE:

Basic

LEARNING OBJECTIVES: PCALC.CO.H.LO.01.01.08 - Evaluate functions for given values of the independent variable.

OTHER:

Bimodal

NOTES:

SCalcET7 Section 1.2 SCalc7e Section 1.2

DATE CREATED:

7/20/2015 1:44 PM

DATE MODIFIED:

1/18/2021 10:33 AM

1.2 A Catalog of Essential Functions

2. Scientists have discovered that a linear relationship exists between the amount of flobberworm mucus secretions and the air temperature. When the temperature is 45°F, the flobberworms each secrete 8.5 grams of mucus a day; when the temperature is 75°F, they each secrete 11.5 grams of mucus a day. Find a function $M(t)$ that gives the amount of mucus secreted on a given day, where t is the temperature of that day in degrees Fahrenheit.

a. $M(t) = 0.1t + 8.5$

b. $M(t) = 10t + 8.5$

c. $M(t) = 10t + 4$

d. $M(t) = 0.1t + 4$

ANSWER: d

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.2.15a SCalc7e 1.2.15a

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.11 - Express a function algebraically, given its verbal or numerical representation.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.2 SCalc7e Section 1.2

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 7/20/2015 1:44 PM

1.2 A Catalog of Essential Functions

3. The relationship between the Fahrenheit and Celsius temperature scales is given by the linear function.

$$F = \frac{9}{5}C + 32$$

What is the F -intercept and what does it represent?

- a. $\frac{9}{5}$, Fahrenheit temperature corresponding to 0°C
- b. $\frac{9}{5}$, Celsius temperature corresponding to 32°C
- c. 32, Celsius temperature corresponding to 0°F
- d. 0, Fahrenheit temperature corresponding to 32°C
- e. 32, Fahrenheit temperature corresponding to 0°C

ANSWER: e

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.2.13a SCalc7e 1.2.13a

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: False

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.02.01.06 - Find the zeros of a polynomial function algebraically.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.2 SCalc7e Section 1.2

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 3:43 AM

1.2 A Catalog of Essential Functions

4. The monthly cost of driving a car depends on the number of miles driven. Julia found that in October it cost her \$300 to drive 400 mi and in July it cost her \$450 to drive 700 mi. Express the monthly cost C as a function of the distance driven d assuming that a linear relationship gives a suitable model.
- a. $C = -100d + 0.5$
 - b. $C = 100d - 0.5$
 - c. $C = 0.5d + 100$
 - d. $C = 2d + 100$
 - e. $C = 0.5d - 100$

ANSWER: c

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.2.18 SCalc7e 1.2.18

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.11 - Express a function algebraically, given its verbal or numerical representation.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.2 SCalc7e Section 1.2

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 7/20/2015 1:44 PM

1.2 A Catalog of Essential Functions

5. Classify the function as a Polynomial function, a Rational function, an algebraic function, or other.

$$f(x) = x^9 + 4x^6 - 6$$

- a. Other
- b. Algebraic
- c. Polynomial
- d. Rational

ANSWER: c
POINTS: 1
DIFFICULTY: Easy
REFERENCES: SCalcET7 1.2.1 SCalc7e 1.2.1
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.02.01.01 - Define polynomial function.
OTHER: Bimodal
NOTES: SCalcET7 Section 1.2 SCalc7e Section 1.2
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 2/17/2020 2:11 AM

1.2 A Catalog of Essential Functions

6. It makes sense that the larger the area of a region, the larger the number of species that inhabit the region. Many ecologists have modeled the species-area relation with a power function and, in particular, the number of species S of bats living in caves in central Mexico has been related to the surface area A measured in m^2 of the caves by the equation

$$S = 0.7A^{0.3}$$

- (a) The cave called mission impossible near puebla, mexico, has surface area of $A = 50m^2$.

How many species of bats would expect to find in that cave?

- (b) If you discover that 3 species of bats live in cave estimate the area of the cave.

ANSWER:
a) 2 species
b) $128 m^2$

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.2.26 SCalc7e 1.2.26

QUESTION TYPE: Numeric Response

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.CO.H.LO.01.01.08 - Evaluate functions for given values of the independent variable.

OTHER: Numerical Response

NOTES: SCalcET7 Section 1.2 SCalc7e Section 1.2

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 4/27/2022 1:51 PM

1.2 A Catalog of Essential Functions

7. The relationship between the Fahrenheit and Celsius temperature scales is given by the linear function.

$$F = \frac{9}{5}C + 32$$

Complete the table and find the slope. Round your answers to the nearest whole number.

°C	°F
15	
-15	
slope	

ANSWER: (15, 59), (-15, 5); slope = 2

POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.2.13b SCalc7e 1.2.13b
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.02.11 - Solve applied problems involving rates of change.
OTHER: Numerical Response
NOTES: SCalcET7 Section 1.2 SCalc7e Section 1.2
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 2/17/2020 2:17 AM

1.2 A Catalog of Essential Functions

8. Find the domain of the function

$$f(x) = \frac{1}{\sqrt{3} - 2\cos x}$$

a. $x \neq \frac{\pi}{6} + 2\pi n$ and $x \neq \frac{11\pi}{6} + 2\pi n$, where n is any integer

b. $x \neq \frac{11\pi}{6}$ and $x \neq \frac{11\pi}{6}$

c. $x \neq \frac{5\pi}{6} + 2\pi n$ and $x \neq \frac{7\pi}{6} + 2\pi n$, where n is any integer

d. $x \neq \frac{5\pi}{6}$ and $x \neq \frac{7\pi}{6}$

e. $x \neq \frac{\pi}{4} + 2\pi n$ and $x \neq \frac{7\pi}{4} + 2\pi n$, where n is any integer

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.02 - Define domain of a function.

DATE CREATED: 3/22/2016 9:17 AM

DATE MODIFIED: 2/5/2021 9:41 AM

9. If the recommended adult dosage for a drug is D (in mg), then to determine the appropriate dosage c for a child of age a , pharmacists use the equation $c = 0.04D(a + 1)$. Suppose the dosage for an adult is 900 mg. What is the slope of the graph of c and what does it represent?

a. 36 mg/yr; the rate of change of dosage with respect to age

b. 36 yr/mg; the rate of change of age with respect to dosage

c. 0.04 mg/yr; the rate of change of dosage with respect to age

d. 0.04 mg/yr; the rate of change of age with respect to dosage

e. 36 mg; the dosage for a newborn

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.01.02.11 - Solve applied problems involving rates of change.

DATE CREATED: 3/23/2016 1:57 AM

DATE MODIFIED: 1/29/2020 6:09 AM

1.2 A Catalog of Essential Functions

10. Biologists have noticed that the chirping rate of crickets of a certain species is related to temperature, and the relationship appears to be very nearly linear. A cricket produces 108 chirps per minute at 70°F and 228 chirps per minute at 90°F. Find a linear equation that models the temperature T as a function of the number of chirps per minute N .

a. $T(N) = \frac{1}{6}N + \frac{312}{6}$

b. $T(N) = \frac{1}{6}N - \frac{312}{6}$

c. $T(N) = 6N - 648$

d. $N(T) = 6T - 312$

e. $N(T) = -6T + 312$

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.11 - Express a function algebraically, given its verbal or numerical representation.

DATE CREATED: 3/23/2016 2:10 AM

DATE MODIFIED: 1/29/2020 6:21 AM

11. Classify the following function:

$$f(x) = x^6(9x^4 - 4)$$

- a. Polynomial function
- b. Power function
- c. Trigonometric function
- d. Rational Function
- e. Exponential function

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

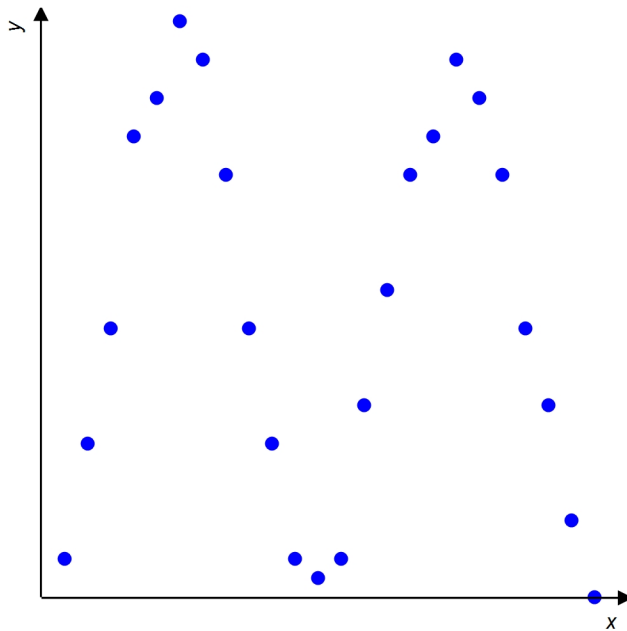
LEARNING OBJECTIVES: PCALC.COH.LO.02.01.01 - Define polynomial function.

DATE CREATED: 3/23/2016 2:28 AM

DATE MODIFIED: 2/17/2020 2:26 AM

1.2 A Catalog of Essential Functions

12. For the scatter plot below, what type of function might you see as a model for the data?



- a. Trigonometric function
- b. Rational Function
- c. Exponential Function
- d. Power Function
- e. Polynomial Function

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.01.03.01 - Identify graphs and properties of common functions.

DATE CREATED: 3/23/2016 2:32 AM

DATE MODIFIED: 2/10/2020 2:17 AM

1.2 A Catalog of Essential Functions

13. Find an equation for the family of linear functions such that $f(6) = 5$.

a. $f(x) = 5 + m(x - 6)$

b. $f(x) = m(x - 6) - 5$

c. $f(x) = 6 + m(x - 5)$

d. $f(x) = m(x + 5) - 5$

e. $f(x) = mx + 6m - 5$

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.CO.H.LO.01.01.11 - Express a function algebraically, given its verbal or numerical representation.

DATE CREATED: 3/23/2016 2:35 AM

DATE MODIFIED: 1/31/2020 12:37 AM

14. The manager of a weekend flea market knows from past experience that if he charges x dollars for a rental space at the market, then the number y of spaces he can rent is given by the equation $y = 560 - 8x$. What does the x -intercept indicate?

a. There will be no spaces occupied when the rental cost is \$70.

b. There will be no spaces occupied when the rental cost is \$560.

c. There will be 560 spaces occupied when there is no rental cost.

d. There will be 8 spaces occupied when there is no rental cost.

e. The number of occupied spaces decreases by 5 for every \$1 increase in rent.

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.CO.H.LO.01.01.10 - Express a function verbally, given its numerical or algebraic representation.

DATE CREATED: 3/23/2016 2:39 AM

DATE MODIFIED: 1/29/2020 6:55 AM

1.2 A Catalog of Essential Functions

15. At the surface of the ocean, the water pressure is the same as the air pressure above the water, 13 lb/in^2 . Below the surface, the water pressure increases by 4.34 lb/in^2 for every 10 ft of descent. At approximately what depth is the pressure 120 lb/in^2 ?
- a. 247 ft
 - b. 276 ft
 - c. 30 ft
 - d. 56 ft
 - e. 359 ft

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

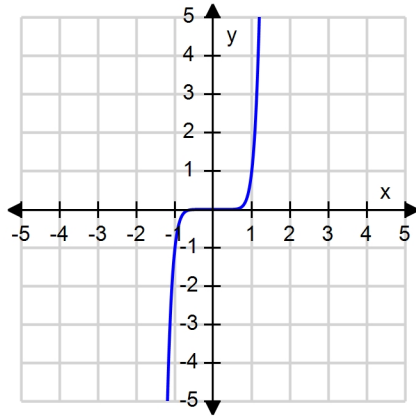
LEARNING OBJECTIVES: PCALC.COH.LO.01.01.12 - Express a function numerically, given its verbal, algebraic, or graphical representation.

DATE CREATED: 3/23/2016 2:46 AM

DATE MODIFIED: 1/29/2020 7:27 AM

1.2 A Catalog of Essential Functions

16. What is the equation of this graph?



- a. $y = x^4$
- b. $y = x^8$
- c. $y = x^{10}$
- d. $y = \sqrt[3]{x}$
- e. $y = x^9$

ANSWER: e
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.40 SCalc7e 1.1.40
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.02.01.10 - Write an equation for a polynomial function, given its graph.
OTHER: Bimodal
NOTES: SCalcET7 Section 1.1 SCalc7e 1.1.40
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 7/31/2020 9:16 AM

1.2 A Catalog of Essential Functions

17. Find the domain of the function.

$$f(x) = \frac{7x + 5}{x^2}$$

a. $(-\infty, 0)$

b. $\left(-\infty, -\frac{5}{7}\right) \cup \left(-\frac{5}{7}, \infty\right)$

c. $\left(-\infty, \frac{5}{7}\right) \cup \left(\frac{5}{7}, \infty\right)$

d. $(-\infty, 0) \cup (0, \infty)$

ANSWER: d

POINTS: 1

DIFFICULTY: Easy

REFERENCES: SCalcET7 1.1.31 SCalc7e 1.1.31

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.07 - Find the domain of a function algebraically.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 4:08 AM

1.2 A Catalog of Essential Functions

18. Find the domain of the function $f(x) = \frac{x}{7 \sin x - 8}$

- a. $(-\infty, \infty)$
- b. $[\frac{8}{7}, \infty)$
- c. $[-8, 7]$
- d. $[-7, 8]$

ANSWER: a

POINTS: 1

DIFFICULTY: Easy

REFERENCES: SCalcET7 1.1.32 SCalc7e 1.1.32

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.07 - Find the domain of a function algebraically.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 2/10/2020 5:53 AM

1.2 A Catalog of Essential Functions

19. Find a , such that the function $f(x) = 4x + \sqrt{a - x^2}$ has the domain $[-3, 3]$.

- a. $a = -9$
- b. $a = \sqrt{3}$
- c. $a = -\sqrt{3}$
- d. $a = 9$
- e. $a = 3$

ANSWER: d

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.38 SCalc7e 1.1.38

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.07 - Find the domain of a function algebraically.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 5:23 AM

1.2 A Catalog of Essential Functions

20. Find the domain.

$$g(u) = \sqrt{u} - \sqrt{3-u}$$

- a. $(0, 3)$
- b. $(-\infty, 0]$
- c. $(-3, \infty]$
- d. $[0, 3]$
- e. $[0, \infty)$

ANSWER: d

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.34 SCalc7e 1.1.34

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.01.07 - Find the domain of a function algebraically.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 5:28 AM

1.2 A Catalog of Essential Functions

21. Find the range of the function.

$$y = 4 + \cos x$$

- a. $(-\infty, \infty)$
- b. $(2, \infty)$
- c. $[-1, 1]$
- d. $(-1, 3)$
- e. $[3, 5]$

ANSWER: e
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.38 SCalc7e 1.1.38
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.05.04.03 - Find the domain and range of the cosine function.
OTHER: Bimodal
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 7/20/2015 1:44 PM

1.2 A Catalog of Essential Functions

22. Find the domain of the function.

$$f(x) = \frac{7}{3x - 1}$$

ANSWER: $\left\{x \mid x \neq \frac{1}{3}\right\}$

POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.31 SCalc7e 1.1.31
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.01.07 - Find the domain of a function algebraically.
OTHER: Numerical Response
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 1/30/2020 8:47 AM

23. Find the domain of the function.

$$f(x) = \sqrt{25 - x^2}$$

ANSWER: $[-5, 5]$
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.38 SCalc7e 1.1.38
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.01.07 - Find the domain of a function algebraically.
OTHER: Numerical Response
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 1/29/2020 5:45 AM

1.2 A Catalog of Essential Functions

24. Find the range of the function.

$$h(x) = \sqrt{36 - x^2}$$

ANSWER: $0 \leq h(x) \leq 6$
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.1.38 SCalc7e 1.1.38
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.01.03 - Define range of a function.
KEYWORDS: 7ET
OTHER: Numerical Response
NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1
DATE CREATED: 7/20/2015 1:44 PM
DATE MODIFIED: 1/19/2021 5:50 AM

25. It makes sense that the larger the area of a region, the larger the number of species that inhabit the region. Many ecologists have modeled the species-area relation with a power function. In particular, the number of species S of bats living in caves in central Mexico has been related to the surface area A of the caves by the equation $S = 0.7A^{0.3}$. If you discover that nine species of bats live in a cave, estimate the area of the cave.

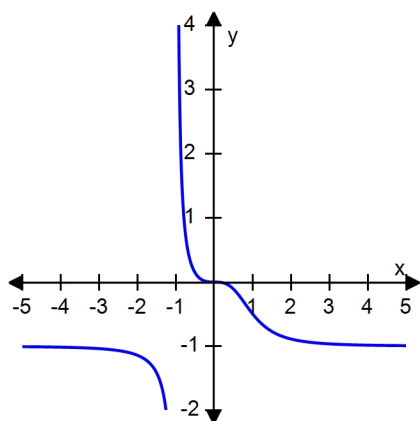
- a. 4979 m²
- b. 1.35 m²
- c. 2125 m²
- d. 2.15 m²

ANSWER: a
POINTS: 1
QUESTION TYPE: Multiple Choice
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.01.08 - Evaluate functions for given values of the independent variable.
DATE CREATED: 1/22/2021 4:49 AM
DATE MODIFIED: 2/12/2021 4:55 AM

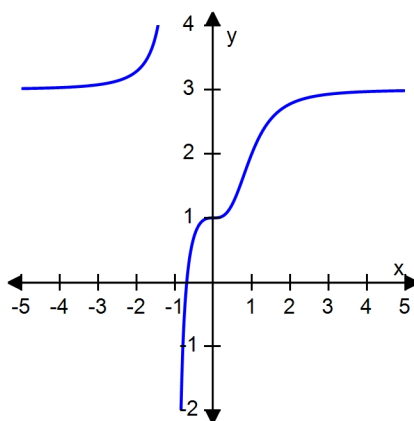
26. Plot the graph of the function f in an appropriate viewing window.

$$f(x) = \frac{x^3}{x^3 + 1}$$

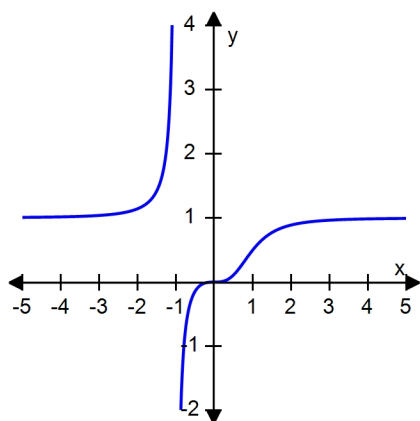
1.2 A Catalog of Essential Functions



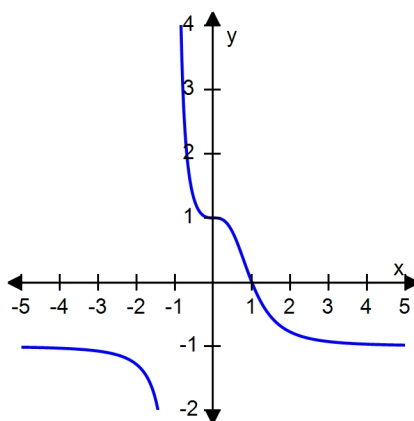
a.



b.



c.



d.

ANSWER: c
POINTS: 1
DIFFICULTY: Easy
REFERENCES: 2.3.50a
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.02.04.11 - Sketch graphs of rational functions using intercepts, asymptotes, zeros, and test values.
KEYWORDS: 7e
OTHER: Bimodal
NOTES: Section 2.3
DATE CREATED: 7/20/2015 3:55 PM
DATE MODIFIED: 2/20/2020 4:30 AM

1.2 A Catalog of Essential Functions

27. Identify the type of the following function.

$$h(r) = 3.6^r$$

- | | |
|-------------------------|---------------------------|
| a. power function | b. root function |
| c. polynomial | d. rational function |
| e. algebraic function | f. trigonometric function |
| g. exponential function | h. logarithmic function |

ANSWER: g

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

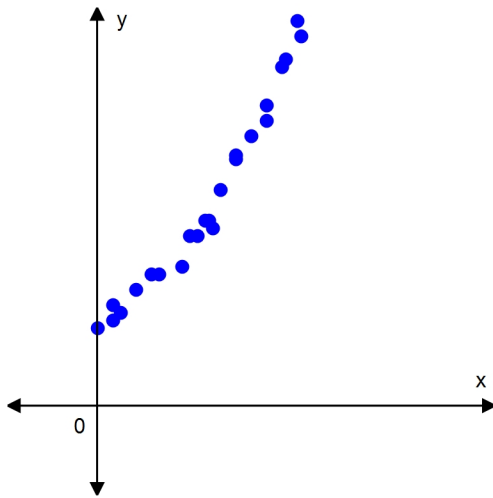
LEARNING OBJECTIVES: PCALC.COH.LO.03.01.01 - Define exponential function.

DATE CREATED: 2/12/2021 5:03 AM

DATE MODIFIED: 2/12/2021 7:41 AM

1.2 A Catalog of Essential Functions

28. Decide what type of function you might choose as a model for the data displayed on the scatter plot.



- a. exponential function
- b. logarithmic function
- c. polynomial
- d. rational function
- e. trigonometric function

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.01 - Define exponential function.

DATE CREATED: 2/12/2021 5:12 AM

DATE MODIFIED: 2/12/2021 7:49 AM

1.2 A Catalog of Essential Functions

29. Determine the domain and range of the function $f(x) = 3^x$.

- a. Domain: $(-\infty, \infty)$, range: $(0, \infty)$
- b. Domain: $(0, \infty)$, range: $(-\infty, \infty)$
- c. Domain: $(0, \infty)$, range: $(0, \infty)$
- d. Domain: $(-\infty, \infty)$, range: $(-\infty, \infty)$
- e. Domain: $(-\infty, \infty)$, range: $(3, \infty)$
- f. Domain: $(3, \infty)$, range: $(-\infty, \infty)$

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.CO.H.LO.03.01.04 - Find the domain and range of exponential functions.

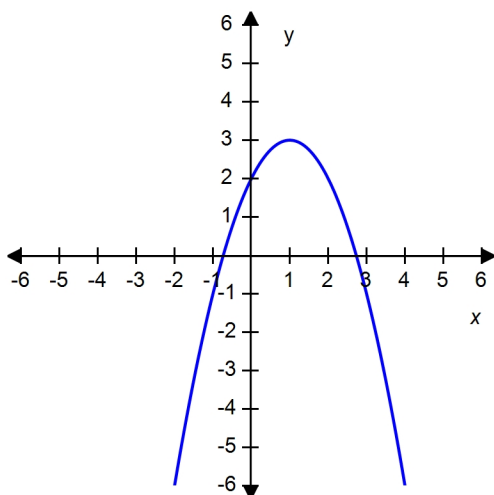
DATE CREATED: 2/12/2021 4:39 AM

DATE MODIFIED: 2/12/2021 7:31 AM

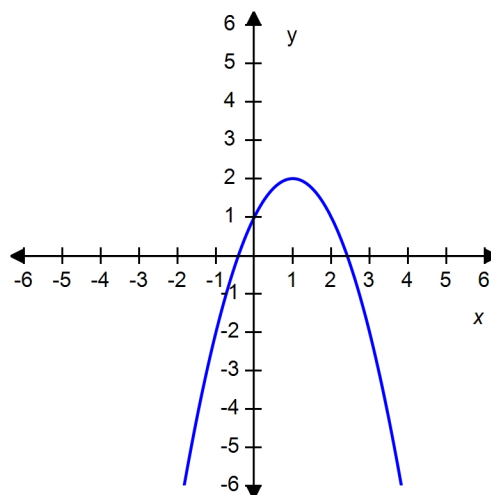
1.3 New Functions from Old Functions

1. Graph the function by hand, not by plotting points, but by starting with the graph of one of the standard functions and then applying the appropriate transformations.

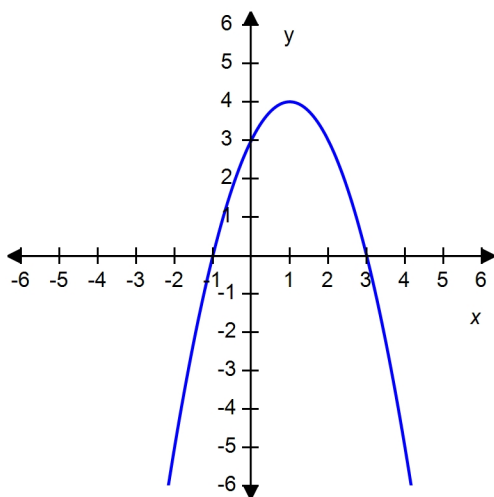
$$y = 3 + 2x - x^2$$



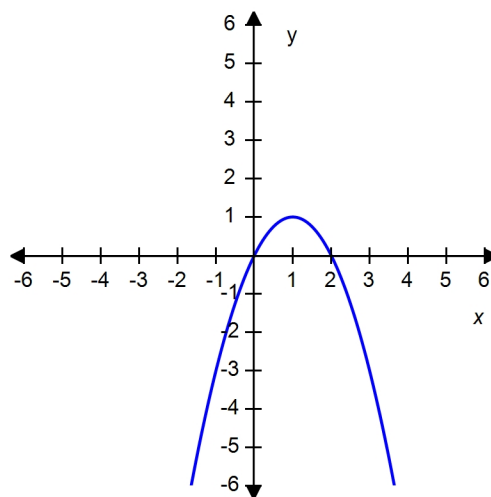
a.



b.



c.



d.

ANSWER: c
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.3.12 SCalc7e 1.3.12
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True

1.3 New Functions from Old Functions

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.03.11 - Sketch the transformed graph of a function, given its transformed equation.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3

DATE CREATED: 7/20/2015 1:45 PM

DATE MODIFIED: 2/24/2020 10:08 AM

2. If $f(x) = x + 15$ and $h(x) = 4x + 85$, find a function g such that $g \circ f = h$.

a. $g(x) = 4x + 25$

b. $g(x) = 4x$

c. $g(x) = x - 25$

d. $g(x) = 4x - 25$

e. $g(x) = x + 25$

ANSWER: a

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.3.61b SCalc7e 1.3.61b

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.06.06 - Combine functions using function composition.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3

DATE CREATED: 7/20/2015 1:45 PM

DATE MODIFIED: 2/5/2020 9:14 AM

1.3 New Functions from Old Functions

3. Use the table to evaluate the expression $(f \circ g)(4)$.

x	1	2	3	4	5	6
$f(x)$	3	2	1	0	1	2
$g(x)$	6	5	2	3	4	6

- a. 4
- b. 1
- c. 2
- d. 3
- e. 5

ANSWER: b
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.3.50f SCalc7e 1.3.50f
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.01.06.06 - Combine functions using function composition.
OTHER: Bimodal
NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3
DATE CREATED: 7/20/2015 1:45 PM
DATE MODIFIED: 3/3/2020 7:11 AM

1.3 New Functions from Old Functions

4. What is $\sqrt[10]{x}$, given that $H = h \circ f \circ g$ and $H(x) = \sqrt[10]{\sqrt{x} - 3}$?

a. $g(x)$

b. $f(x)$

c. $h(x)$

ANSWER: c

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.3.47 SCalc7e 1.3.47

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.06.08 - Identify the functions that make up a composite function.

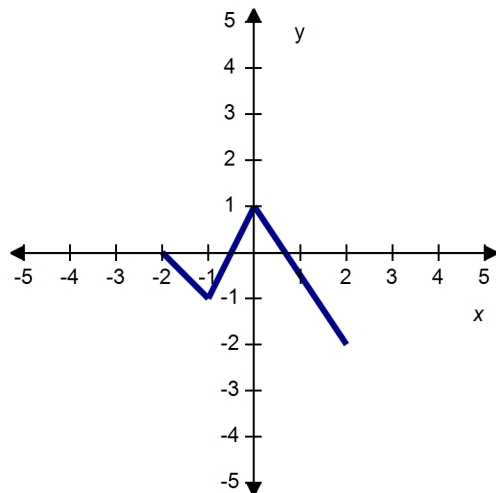
OTHER: Bimodal

NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3

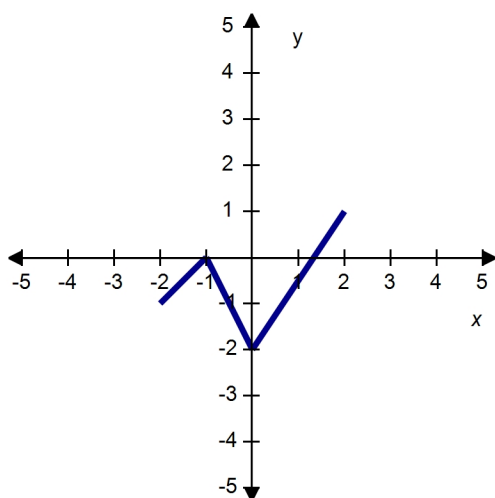
DATE CREATED: 7/20/2015 1:45 PM

DATE MODIFIED: 1/29/2020 11:43 PM

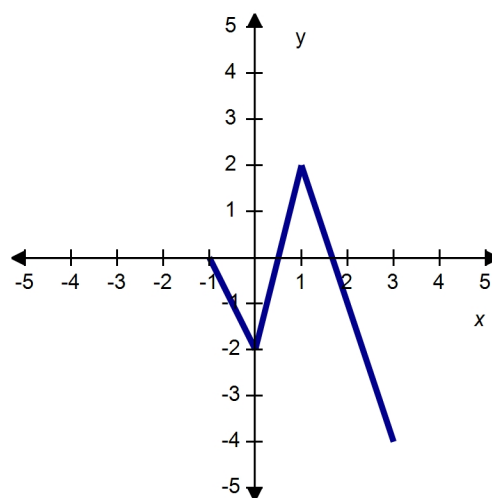
5. The graph of the function f follows. Choose the graph of $y = -f(x) - 1$.



1.3 New Functions from Old Functions



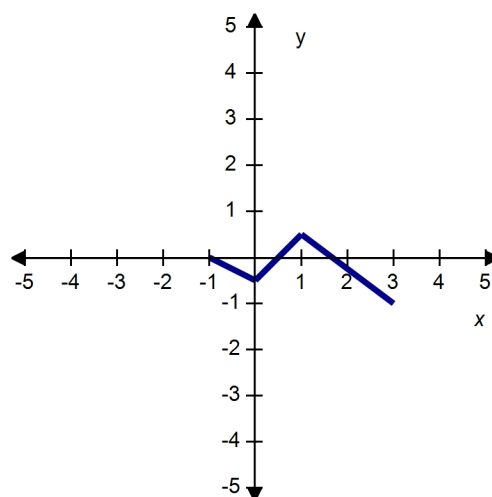
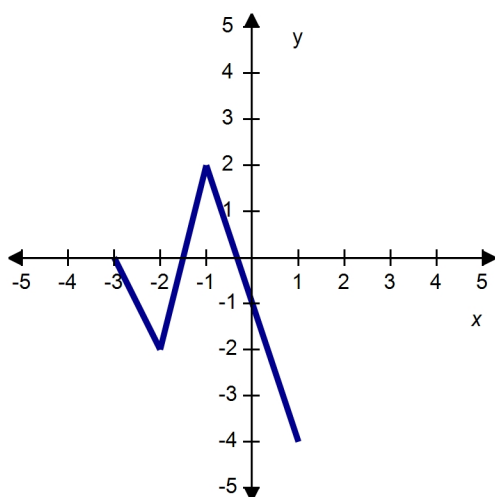
a.



b.

c.

d.



ANSWER: a
 POINTS: 1
 DIFFICULTY: Medium
 REFERENCES: SCalcET7 1.3.5b SCalc7e 1.3.5b
 QUESTION TYPE: Multi-Mode (Multiple choice)
 HAS VARIABLES: True
 STUDENT ENTRY MODE: Basic
 LEARNING OBJECTIVES: PCALC.COH.LO.01.03.11 - Sketch the transformed graph of a function, given its transformed equation.
 OTHER: Bimodal
 NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3
 DATE CREATED: 7/20/2015 1:45 PM

1.3 New Functions from Old Functions

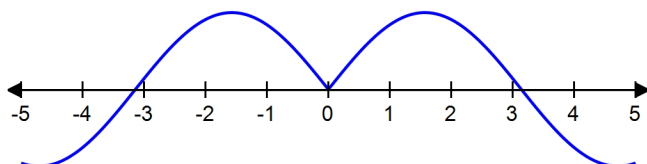
DATE MODIFIED: 3/3/2020 5:50 AM

1.3 New Functions from Old Functions

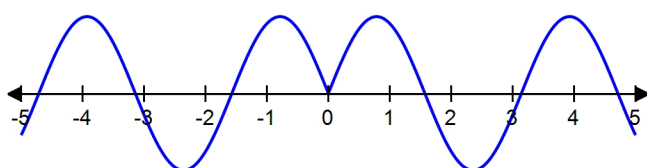
6. Which of the following graphs is the graph of the function?

$$f(x) = \sin|2x|$$

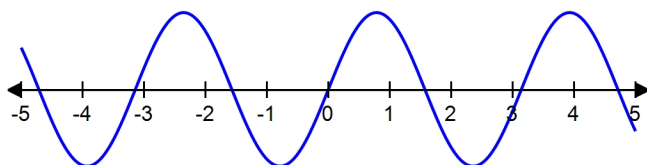
Graph 1



Graph 2



Graph 3



- a. Graph 2
- b. Graph 1
- c. Graph 3

ANSWER:

a

POINTS:

1

DIFFICULTY:

Medium

REFERENCES:

SCalcET7 1.3.24 SCalc7e 1.3.24

QUESTION TYPE:

Multi-Mode (Multiple choice)

HAS VARIABLES:

True

STUDENT ENTRY MODE:

Basic

LEARNING OBJECTIVES: PCALC.CO.H.LO.01.03.11 - Sketch the transformed graph of a function, given its transformed equation.

OTHER:

Bimodal

NOTES:

SCalcET7 Section 1.3 SCalc7e Section 1.3

DATE CREATED:

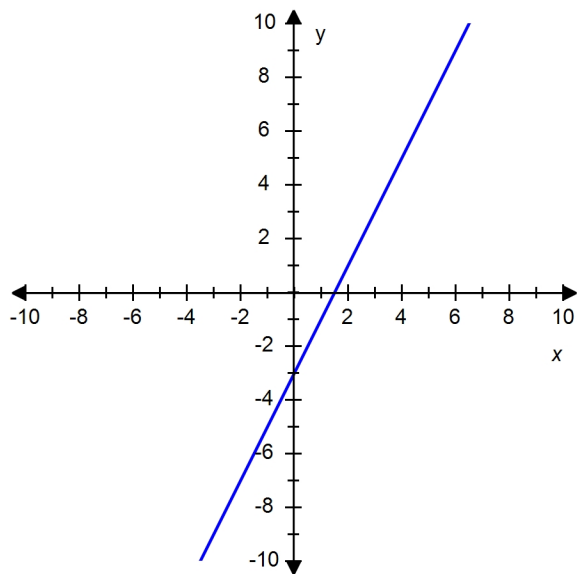
7/20/2015 1:45 PM

DATE MODIFIED:

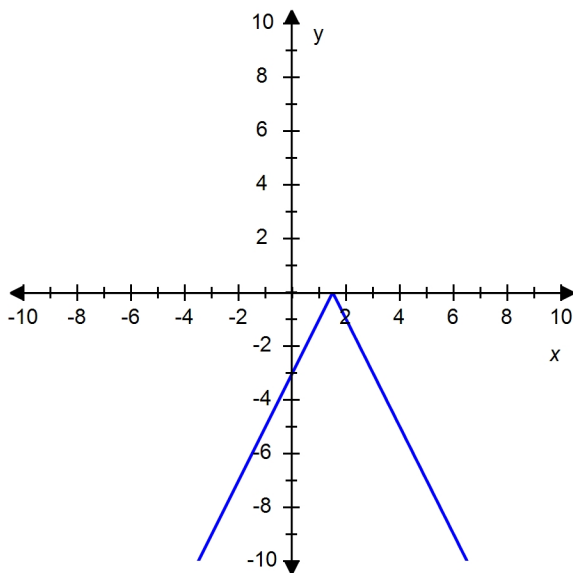
2/5/2020 8:03 AM

1.3 New Functions from Old Functions

7. The graph of the function f follows. Choose the graph of $y = f(|x|)$.

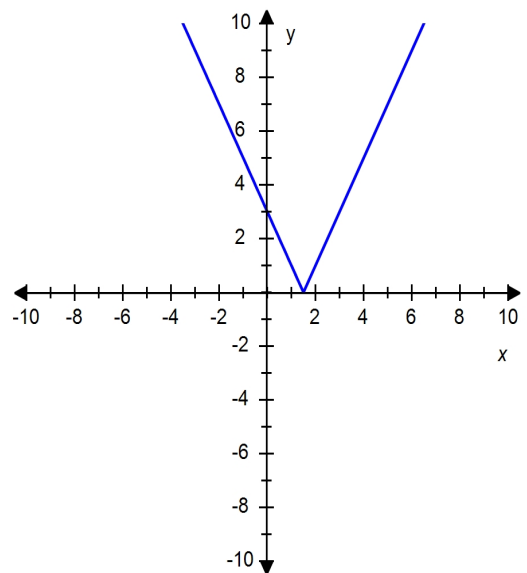


a.



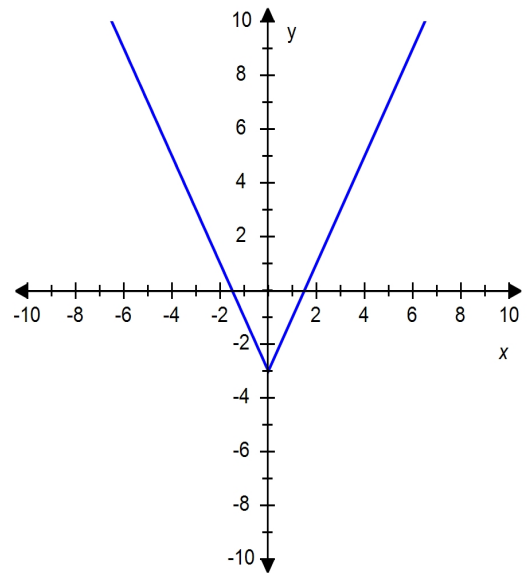
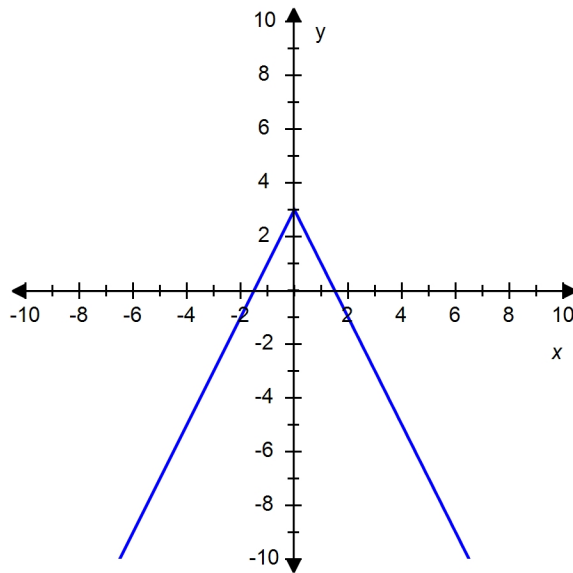
c.

b.



d.

1.3 New Functions from Old Functions



ANSWER: d
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.3.27a SCalc7e 1.3.27a
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.01.03.11 - Sketch the transformed graph of a function, given transformed equation.
OTHER: Bimodal
NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3
DATE CREATED: 7/20/2015 1:45 PM
DATE MODIFIED: 3/4/2020 4:11 AM

1.3 New Functions from Old Functions

8. Suppose that the graph of f is given. Describe how the graph of the function $y = f(x - 3) - 3$ can be obtained from the graph of f .
- a. Shift the graph 3 units to the left and 3 units down.
 - b. Shift the graph 3 units to the left and 3 units up.
 - c. Shift the graph 3 units to the right and 3 units up.
 - d. Shift the graph 3 units to the right and 3 units down.
 - e. None of these

ANSWER: d

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.3.1bc SCalc7e 1.3.1bc

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.03.10 - Describe the transformations applied to the graph of a function, given its transformed equation.

OTHER: Bimodal

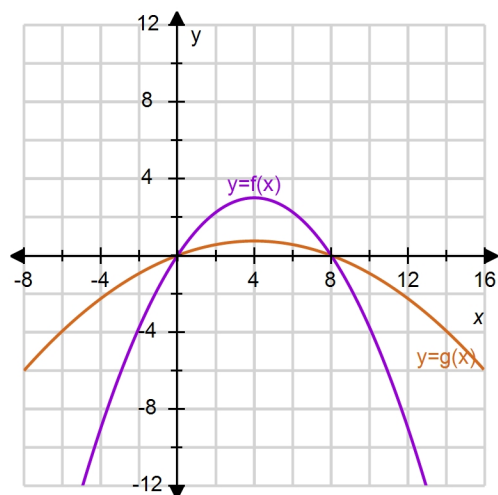
NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3

DATE CREATED: 7/20/2015 1:45 PM

DATE MODIFIED: 7/20/2015 1:45 PM

1.3 New Functions from Old Functions

9. Which of the following is the equation for the function $g(x)$?



- a. $g(x) = 4f(x)$
- b. $g(x) = f(x) - 4$
- c. $g(x) = -f(x + 4)$
- d. $g(x) = \frac{f(x)}{4}$
- e. $g(x) = -f(x) + 4$

ANSWER: d

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.3.3c SCalc7e 1.3.3c

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.CO.H.LO.01.03.14 - Write an equation for a given transformed graph of a common function.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3

DATE CREATED: 7/20/2015 1:45 PM

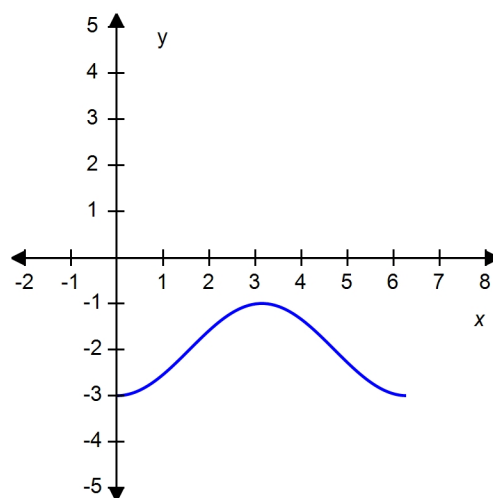
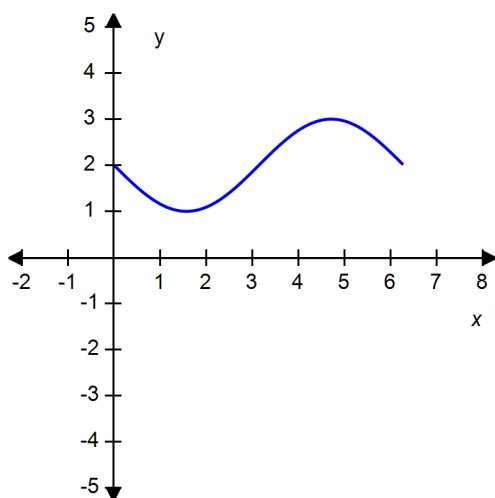
DATE MODIFIED: 2/5/2020 8:16 AM

10. Sketch the graph of $y = 2 - \cos x$ over one period.

a.

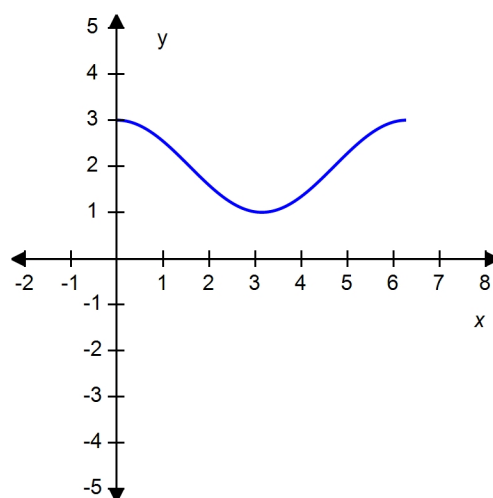
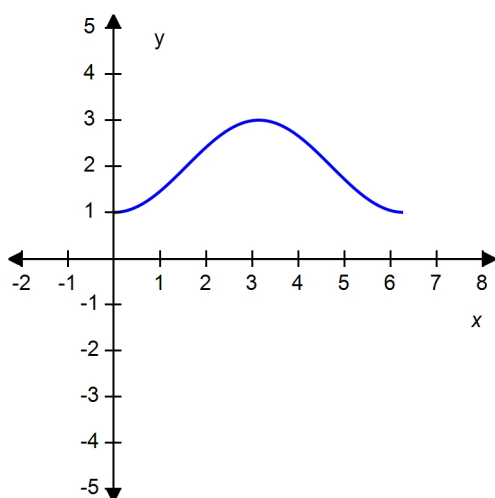
b.

1.3 New Functions from Old Functions



c.

d.



ANSWER: c

POINTS: 1

DIFFICULTY: Easy

REFERENCES: SCalcET7 1.3.27b SCalc7e 1.3.27b

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.03.11 - Sketch the transformed graph of a function, given its transformed equation.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3

1.3 New Functions from Old Functions

DATE CREATED: 7/20/2015 1:45 PM

DATE MODIFIED: 3/3/2020 7:31 AM

11. Find the function $f \circ g$ and its domain if $f(x) = \sqrt{x+6}$ and $g(x) = \sqrt{x-6}$.

a. $\sqrt{x^2 - 36}$
 $D = [6, \infty)$

b. $\sqrt{x^2 - 36}$
 $D = [-6, \infty)$

c. $\sqrt{x^2 + 36}$
 $D = [-6, \infty)$

d. $\sqrt{x^2 + 36}$
 $D = [6, \infty)$

ANSWER: a

POINTS: 1

DIFFICULTY: Easy

REFERENCES: SCalcET7 1.3.29 SCalc7e 1.3.29

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.01.06.07 - Find the domain of a composite function.

OTHER: Bimodal

NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3

DATE CREATED: 7/20/2015 1:45 PM

DATE MODIFIED: 1/18/2021 10:56 AM

1.3 New Functions from Old Functions

12. Find the function $f \circ g$ and its domain if $f(x) = \frac{x-1}{x}$ and $g(x) = \frac{x}{x+5}$.

a. $\frac{x-1}{x+5}, D = (-\infty, -5) \cup (-5, 0) \cup (0, \infty)$

b. $\frac{x-1}{x+5}, D = (-\infty, -5) \cup (-5, \infty)$

c. $-\frac{5}{x}, D = (-\infty, -5) \cup (-5, 0) \cup (0, \infty)$

d. $-\frac{5}{x}, D = (-\infty, 0) \cup (0, \infty)$

ANSWER:

c

POINTS:

1

DIFFICULTY:

Medium

REFERENCES:

SCalcET7 1.3.35a SCalc7e 1.3.35a

QUESTION TYPE:

Multiple Choice

HAS VARIABLES:

True

LEARNING OBJECTIVES:

PCALC.COH.LO.01.06.07 - Find the domain of a composite function.

OTHER:

Bimodal

NOTES:

SCalcET7 Section 1.3 SCalc7e Section 1.3

DATE CREATED:

7/20/2015 1:45 PM

DATE MODIFIED:

1/30/2020 1:34 AM

1.3 New Functions from Old Functions

13. The graph of the function $f(x) = x^2 - 8x + 4$ has been shifted horizontally to the left by 9 units. Find the function for the transformed graph.

- a. $g(x) = x^2 - 8x - 5$
- b. $g(x) = x^2 - 8x + 13$
- c. $g(x) = x^2 + 10x + 13$
- d. $g(x) = x^2 - 26x + 157$

ANSWER: c
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.3.1g SCalc7e 1.3.1g
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.01.03.13 - Write an equation for the transformed graph of a function, given its verbal description.
OTHER: Bimodal
NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3
DATE CREATED: 7/20/2015 1:45 PM
DATE MODIFIED: 2/3/2020 8:40 AM

1.3 New Functions from Old Functions

14. Express the function in the form of $f \circ g \circ h$.

$$H(x) = 3 - 5^{x^3}$$

ANSWER: $h(x) = x^3, g(x) = 5^x, f(x) = 3 - x$

POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.3.48 SCalc7e 1.3.48
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.06.08 - Identify the functions that make up a composite function.
OTHER: Numerical Response
NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3
DATE CREATED: 7/20/2015 1:45 PM
DATE MODIFIED: 1/30/2020 2:34 AM

15. A spherical balloon with radius r inches has volume $4\frac{\pi r^3}{3}$.

Find a function that represents the amount of air required to inflate the balloon from a radius of r inches to a radius of $r + 2$ inches.

ANSWER: $\frac{8}{3} \pi(6r^2 + 12r + 8)$

POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.3.54 SCalc7e 1.3.54
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.03.13 - Write an equation for the transformed graph of a function, given its verbal description.
OTHER: Numerical Response
NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3
DATE CREATED: 7/20/2015 1:45 PM
DATE MODIFIED: 2/5/2020 8:53 AM

1.3 New Functions from Old Functions

16. Express the function in the form of $f \circ g$.

$$v(t) = \tan(t^2)\sin(t^2)$$

ANSWER: $f(t) = \tan(t)\sin(t)$
 $g(t) = t^2$
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.3.45 SCalc7e 1.3.45
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.06.08 - Identify the functions that make up a composite function.
OTHER: Numerical Response
NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3
DATE CREATED: 7/20/2015 1:45 PM
DATE MODIFIED: 1/18/2021 10:56 AM

17. A stone is dropped into a lake, creating a circular ripple that travels outward at a speed of 49 cm/s. Express the radius r of this circle as a function of the time t (in seconds) and find $A \circ r$, if A is the area of this circle as a function of the radius.

ANSWER: $r(t) = 49t, 2401 \pi t^2$
POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.3.53 SCalc7e 1.3.53
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.06.09 - Solve applied problems involving combinations of functions.
OTHER: Numerical Response
NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3
DATE CREATED: 7/20/2015 1:45 PM
DATE MODIFIED: 1/30/2020 3:55 AM

1.3 New Functions from Old Functions

18. Let $f(x) = x^2 - 18x + 81$ and $g(x) = \sqrt{x + 1}$. Find $(f \circ g)(12)$.

ANSWER: 0
POINTS: 1
DIFFICULTY: Easy
REFERENCES: SCalcET7 1.3.36 SCalc7e 1.3.36
QUESTION TYPE: Subjective Short Answer
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.01.06.06 - Combine functions using function composition.
OTHER: Short Answer
NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3
DATE CREATED: 7/20/2015 1:45 PM
DATE MODIFIED: 3/4/2020 5:38 AM

19. Find $f \circ g \circ h$ if

$$f(x) = \sqrt{x}, \quad g(x) = 3x + 1, \quad \text{and} \quad h(x) = x^2 - 1$$

ANSWER: $\sqrt{3x^2 - 2}$

POINTS: 1
DIFFICULTY: Medium
REFERENCES: SCalcET7 1.3.37 SCalc7e 1.3.37
QUESTION TYPE: Subjective Short Answer
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.01.06.06 - Combine functions using function composition.
OTHER: Short Answer
NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3
DATE CREATED: 7/20/2015 1:45 PM
DATE MODIFIED: 2/10/2020 6:25 AM

1.3 New Functions from Old Functions

20. Find the function g such that $h(x) = (g \circ f)(x)$.

$$h(x) = \sin^5 x \text{ and } f(x) = \sin x$$

ANSWER: $g(x) = x^5$

POINTS: 1

DIFFICULTY: Easy

REFERENCES: SCalcET7 1.3.62 SCalc7e 1.3.62

QUESTION TYPE: Subjective Short Answer

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.06.08 - Identify the functions that make up a composite function.

OTHER: Short Answer

NOTES: SCalcET7 Section 1.3 SCalc7e Section 1.3

DATE CREATED: 7/20/2015 1:45 PM

DATE MODIFIED: 1/30/2020 4:22 AM

1.4 Exponential Functions

1. Use the Law of Exponents to rewrite and simplify the expression.

$$\frac{\sqrt{a\sqrt{b}}}{\sqrt[6]{ab}}$$

a. $\left(\frac{a}{b}\right)^{\frac{1}{3}}$

b. $\frac{a^{\frac{1}{3}}}{b^{\frac{1}{12}}}$

c. $\frac{a}{b}$

d. $\frac{a}{b^{\frac{1}{12}}}$

e. $a^{\frac{1}{3}} b^{\frac{1}{12}}$

ANSWER:	e
POINTS:	1
DIFFICULTY:	Medium
REFERENCES:	1.5.4b
QUESTION TYPE:	Multiple Choice
HAS VARIABLES:	True
LEARNING OBJECTIVES:	PCALC.CO.H.LO.03.01.01 - Define exponential function.
KEYWORDS:	7ET
OTHER:	Bimodal
NOTES:	Section 1.5
DATE CREATED:	7/20/2015 1:45 PM
DATE MODIFIED:	2/10/2020 5:38 AM

1.4 Exponential Functions

2. Starting with the graph of $y = e^x$, find the equation of the graph that results from reflecting about the line $y = 5$.

- a. $y = -e^x$
- b. $y = -e^x + 10$
- c. $y = -e^{-5x} + 10$
- d. $y = e^{-x} + 10$
- e. $y = -e^{x+10}$

ANSWER: b
POINTS: 1
DIFFICULTY: Medium
REFERENCES: 1.5.18a
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.03.01.06 - Given its graph, write an equation for an exponential function.
KEYWORDS: 7ET
OTHER: Bimodal
NOTES: Section 1.5
DATE CREATED: 7/20/2015 1:45 PM
DATE MODIFIED: 1/29/2020 4:19 AM

1.4 Exponential Functions

3. Use the Law of Exponents to rewrite and simplify the expression.

$$\frac{x^{4n} \cdot x^{5n+1}}{x^{n-4}}$$

a. x^{8n+5}

b. x^{8n+6}

c. x^{6n-9}

d. x^{3n+8}

e. x^{4n-7}

ANSWER: a

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 1.5.4a

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.01 - Define exponential function.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: Section 1.5

DATE CREATED: 7/20/2015 1:45 PM

DATE MODIFIED: 1/29/2020 4:43 AM

1.4 Exponential Functions

4. Starting with the graph of $y = e^x$, write the equation of the graph that results from shifting 6 units right.

a. $y = e^{x+6}$

b. $y = e^x - 6$

c. $y = e^{x-6}$

d. $y = e^x + 6$

e. $y = 6e^{x-6}$

ANSWER: c

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 1.5.18b

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.06 - Given its graph, write an equation for an exponential function.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: Section 1.5

DATE CREATED: 7/20/2015 1:45 PM

DATE MODIFIED: 1/29/2020 4:53 AM

1.4 Exponential Functions

5. The table gives the population of the United States, in millions, for the years 1900 - 2000. Use a graphing calculator with exponential regression capability to model the U.S. population since 1900. Use the model to estimate the population in 1965 and to predict the population in the year 2025.

Year	1900	1910	1920	1930	1940	1950	1960	1970	1980	1990	2000
Population (millions)	76	92	106	123	131	150	179	203	227	250	281

- a. 185 million, 400 million
- b. 190 million, 405 million
- c. 195 million, 410 million
- d. 180 million, 395 million
- e. 175 million, 390 million

ANSWER: a

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 1.5.32

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.10 - Solve applied problems involving exponential functions.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: Section 1.5

DATE CREATED: 7/20/2015 1:45 PM

DATE MODIFIED: 7/20/2015 1:45 PM

1.4 Exponential Functions

6. Under ideal conditions a certain bacteria population is known to double every three hours. Suppose that there are initially 20 bacteria. What is the size of the population after 15 hours?
- a. 1,280 bacteria
 - b. 80 bacteria
 - c. 640 bacteria
 - d. 160 bacteria
 - e. 320 bacteria

ANSWER: c

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 1.5.29a

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.10 - Solve applied problems involving exponential functions.

KEYWORDS: 7ET

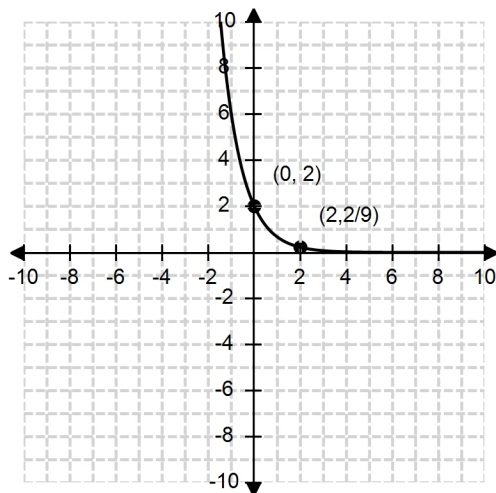
OTHER: Bimodal

NOTES: Section 1.5

DATE CREATED: 7/20/2015 1:45 PM

DATE MODIFIED: 7/20/2015 1:45 PM

7. Find the exponential function $y = Ca^x$ whose graph is given.



a. $f(x) = 2\left(\frac{1}{3}\right)^x$

1.4 Exponential Functions

b. $f(x) = 3\left(\frac{1}{3}\right)^x$

c. $f(x) = \left(\frac{3}{2}\right)^x$

d. $f(x) = \frac{1}{3^x}$

e. $f(x) = \left(\frac{3}{4}\right)^x$

ANSWER: a
POINTS: 1
DIFFICULTY: Medium
REFERENCES: 1.5.21
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.03.01.06 - Given its graph, write an equation for an exponential function.
KEYWORDS: 7ET
OTHER: Bimodal
NOTES: Section 1.5
DATE CREATED: 7/20/2015 1:45 PM
DATE MODIFIED: 2/10/2020 4:47 AM

1.4 Exponential Functions

8. The half-life of bismuth-210, ^{210}Bi , is 5 days. If a sample has a mass of 600 mg, find the amount remaining after 4 weeks. Round your answer to one decimal place.

- a. 12.4 mg
- b. 29,102 mg
- c. 0 mg
- d. 82.8 mg
- e. 6,000 mg

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.10 - Solve applied problems involving exponential functions.

DATE CREATED: 3/22/2016 9:17 AM

DATE MODIFIED: 3/23/2016 8:17 AM

9. An isotope of sodium, ^{24}Na , has a half-life of 15 hours. A sample of this isotope has mass 9 g. Estimate the time required for the mass to be reduced to 0.5 g.

- a. 62.5 hours
- b. 2.1 hours
- c. 70.3 hours
- d. 47.5 hours
- e. 125.1 hours

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.10 - Solve applied problems involving exponential functions.

DATE CREATED: 3/22/2016 9:32 AM

DATE MODIFIED: 1/18/2021 4:44 AM

1.4 Exponential Functions

10. Find the domain of the following function.

$$f(x) = \frac{1 - e^{x^2}}{1 - e^{36 - x^2}}$$

- a. $\mathbb{R}$
- b. $x \neq 0$
- c. $0 < x < 6$
- d. $x \neq \pm 36$
- e. $x \neq \pm 6$

ANSWER: e

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.04 - Find the domain and range of exponential functions.

DATE CREATED: 3/22/2016 9:45 AM

DATE MODIFIED: 1/18/2021 4:43 AM

1.4 Exponential Functions

11. After alcohol is fully absorbed into the body, it is metabolized with a half-life of about 1.25 hours. Suppose you have had three alcoholic drinks and an hour later, at midnight, your blood alcohol concentration (BAC) is 0.6 mg/mL. Find an exponential decay model for your BAC t hours after midnight.

a. $BAC(t) = 0.6 \cdot (2)^{-\frac{4t}{5}}$

b. $BAC(t) = 1.25 \cdot (2)^{-\frac{t}{0.6}}$

c. $BAC(t) = 0.6 \cdot \left(\frac{1}{2}\right)^{1.25t}$

d. $BAC(t) = 1.25 \cdot \left(\frac{1}{2}\right)^{0.6t}$

e. None of the above

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.10 - Solve applied problems involving exponential functions.

DATE CREATED: 3/22/2016 9:57 AM

DATE MODIFIED: 1/18/2021 4:44 AM

1.4 Exponential Functions

12. Determine the range of the following function.

$$g(x) = -2^{-x} - 9$$

- a. $(-\infty, -9)$
- b. $(9, \infty)$
- c. $\mathbb{R}$
- d. $(-9, \infty)$
- e. $(0, -\infty)$

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.04 - Find the domain and range of exponential functions.

DATE CREATED: 3/22/2016 10:11 AM

DATE MODIFIED: 1/18/2021 4:44 AM

13. Use the Law of Exponents to rewrite and simplify the expression.

$$\frac{(4z^8)^8}{2z^9}$$

- a. $32,768z^{55}$
- b. $65,536z^{55}$
- c. $32,768z^8$
- d. $2z^{55}$
- e. $2z^8$

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.01 - Define exponential function.

DATE CREATED: 3/22/2016 10:17 AM

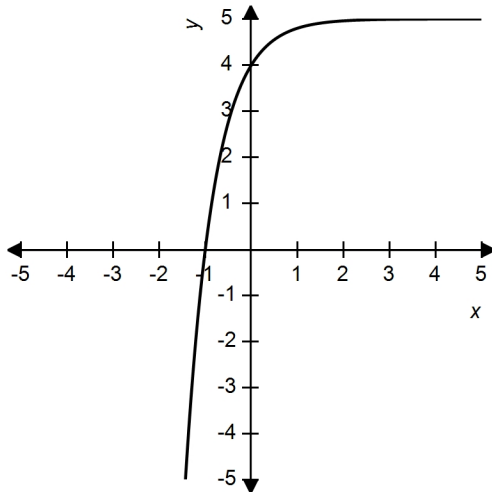
DATE MODIFIED: 1/29/2020 5:50 AM

14. Identify the graph of the following function.

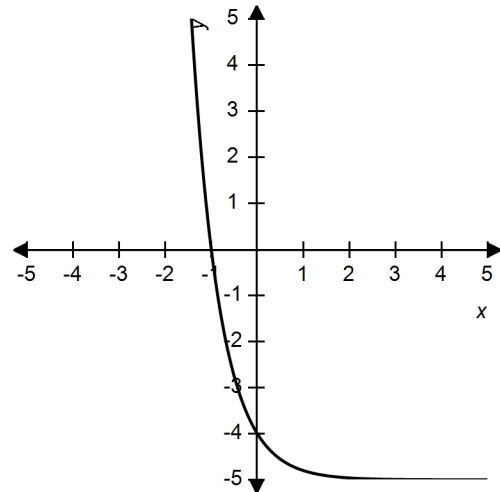
1.4 Exponential Functions

$$y = 5 - (0.2)^x$$

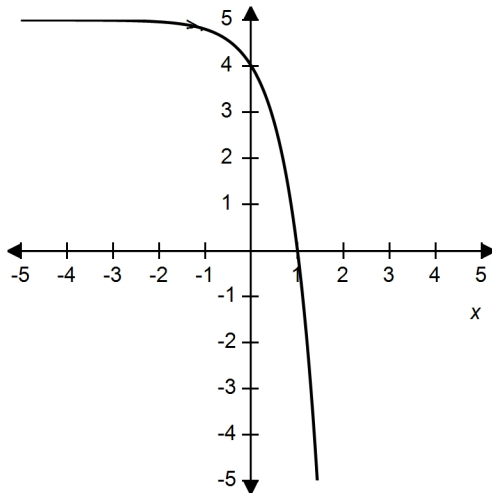
a.



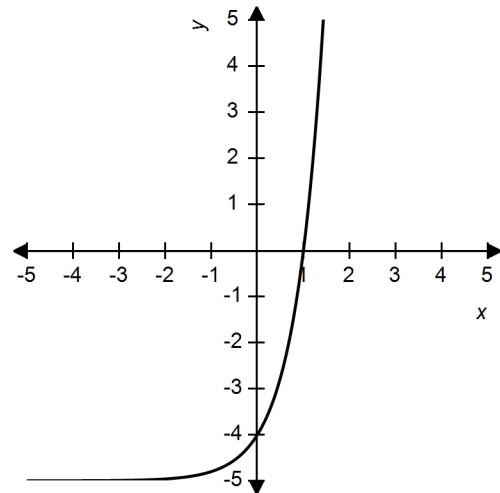
b.



c.



d.



ANSWER:

a

POINTS:

1

QUESTION TYPE:

Multiple Choice

HAS VARIABLES:

True

LEARNING OBJECTIVES: PCALC.CO.H.LO.03.01.07 - Sketch graphs of transformations of exponential functions.

DATE CREATED:

3/22/2016 10:27 AM

DATE MODIFIED:

2/10/2020 4:48 AM

1.4 Exponential Functions

15. Starting with the graph of $y = e^x$, write the equation of the graph that results from shifting 7 units to the left and 6 units upward.

a. $y = e^{x+7} + 6$

b. $y = e^{x+6} + 7$

c. $y = e^{x+7} - 6$

d. $y = e^{x-7} + 6$

e. $y = 6e^{x-7}$

ANSWER: a

POINTS: 1

QUESTION TYPE: Multiple Choice

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.06 - Given its graph, write an equation for an exponential function.

DATE CREATED: 3/22/2016 10:40 AM

DATE MODIFIED: 1/29/2020 5:48 AM

16. Find the domain of the function.

$$f(x) = \frac{3}{1 - e^x}$$

ANSWER: $(-\infty, 0) \cup (0, \infty)$

POINTS: 1

DIFFICULTY: Medium

REFERENCES: SCalcET7 1.1.42 SCalc7e 1.1.42

QUESTION TYPE: Numeric Response

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.04 - Find the domain and range of exponential functions.

OTHER: Numerical Response

NOTES: SCalcET7 Section 1.1 SCalc7e Section 1.1

DATE CREATED: 7/20/2015 1:44 PM

DATE MODIFIED: 1/29/2020 5:47 AM

1.5 Logarithms

1. Determine whether the function is one-to-one.

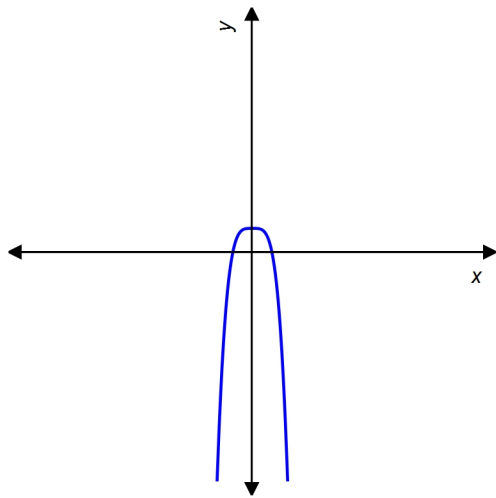
$$f(x) = \sqrt{4 - x}$$

- a. No
b. Yes

ANSWER: b
POINTS: 1
DIFFICULTY: Easy
REFERENCES: 1.6.9
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.01.05.03 - Given its equation, determine if a function is one-to-one.
KEYWORDS: 7ET
OTHER: Bimodal
NOTES: Section 1.6
DATE CREATED: 7/20/2015 1:46 PM
DATE MODIFIED: 1/30/2020 5:13 AM

1.5 Logarithms

2. Determine whether f is one-to-one.



ANSWER: No

POINTS: 1

DIFFICULTY: Easy

REFERENCES: 1.6.5

QUESTION TYPE: Subjective Short Answer

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.05.02 - Given its graph, determine if a function is one-to-one using the horizontal line test.

KEYWORDS: 7ET

OTHER: Short Answer

NOTES: Section 1.6

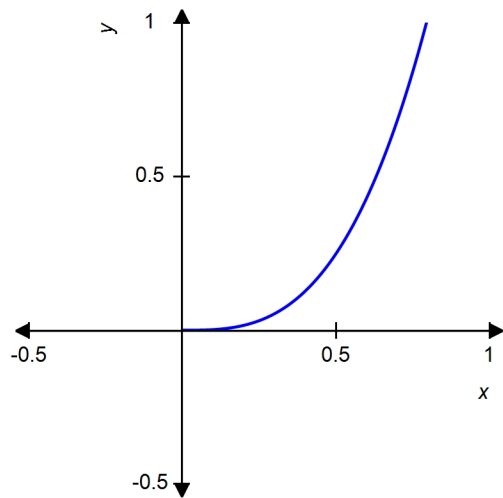
DATE CREATED: 7/20/2015 1:46 PM

DATE MODIFIED: 2/5/2020 8:21 AM

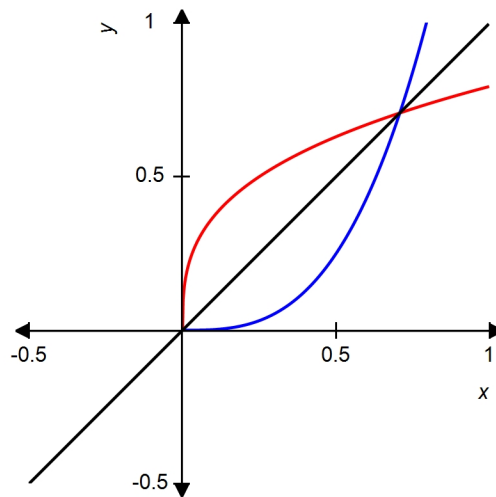
3. The graph of f is given. Sketch the graph of f^{-1} on the same set of axes.

$$y = f(x)$$

1.5 Logarithms



ANSWER: $y = f(x)$ - blue, $y = f^{-1}(x)$ -red



POINTS: 1
DIFFICULTY: Easy
REFERENCES: 1.6.30
QUESTION TYPE: Subjective Short Answer
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.01.05.06 - Given the graph of a one-to-one function, sketch the graph of its inverse using symmetry.
KEYWORDS: 7ET
OTHER: Short Answer
NOTES: Section 1.6

1.5 Logarithms

DATE CREATED: 7/20/2015 1:46 PM
DATE MODIFIED: 2/10/2020 12:41 AM

4. Find $f^{-1}(a)$ for the function f and the real number a .

$$f(x) = x^3 + x - 2; a = -4$$

- a. 0
- b. -1
- c. -2
- d. 1

ANSWER: b
POINTS: 1
DIFFICULTY: Medium
REFERENCES: 1.6.16
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.01.05.09 - Evaluate the inverse of a one-to-one function given its numerical, algebraic, or graphical representation.
KEYWORDS: 7ET
OTHER: Bimodal
NOTES: Section 1.6
DATE CREATED: 7/20/2015 1:46 PM
DATE MODIFIED: 1/30/2020 5:22 AM

1.5 Logarithms

5. Find the inverse function of $f(x) = \frac{x + 1}{5x + 1}$.

a. $f^{-1}(x) = -(x + 1)(5x + 1)$

b. $f^{-1}(x) = -\frac{5x + 1}{x - 1}$

c. $f^{-1}(x) = -\frac{x - 1}{5x - 1}$

d. $f^{-1}(x) = \frac{x}{5x - 1}$

e. $f^{-1}(x) = (x + 1)(5x + 1)$

ANSWER: c

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 1.6.22

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.05.10 - Find the inverse of a function algebraically.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: Section 1.6

DATE CREATED: 7/20/2015 1:46 PM

DATE MODIFIED: 1/30/2020 5:02 AM

6. Find the inverse of f . Then sketch the graphs of f and f^{-1} on the same set of axes.

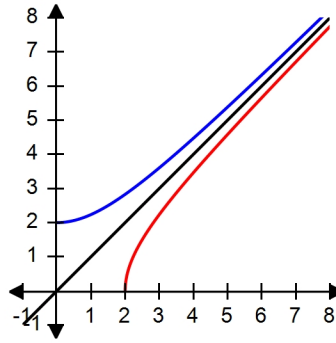
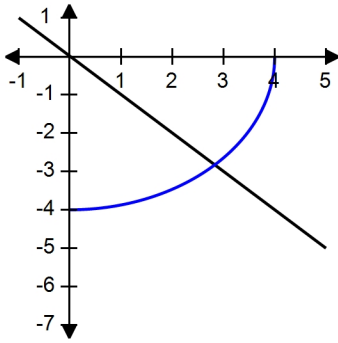
$$f(x) = \sqrt{16 - x^2}, x \geq 0$$

a. $f^{-1}(x) = -\sqrt{16 - x^2}, x \geq 0$ b. $f^{-1}(x) = \sqrt{4 + x^2}, x \geq 0$

$$f = f^{-1}$$

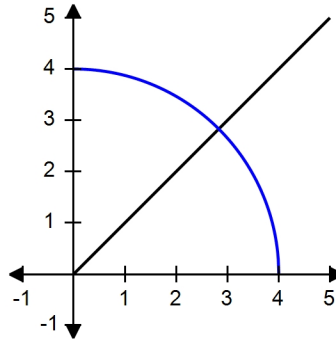
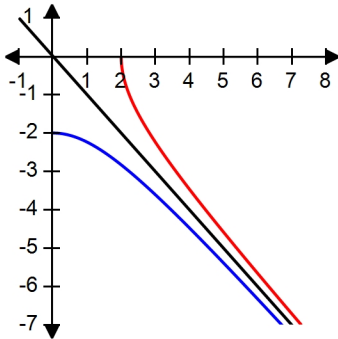
$$f(\text{blue}), f^{-1}(\text{red})$$

1.5 Logarithms



c. $f^{-1}(x) = -\sqrt{4 + x^2}, x \geq 0$
 $f(\text{blue}), f^{-1}(\text{red})$

d. $f^{-1}(x) = \sqrt{16 - x^2}, x \geq 0$
 $f = f^{-1}$



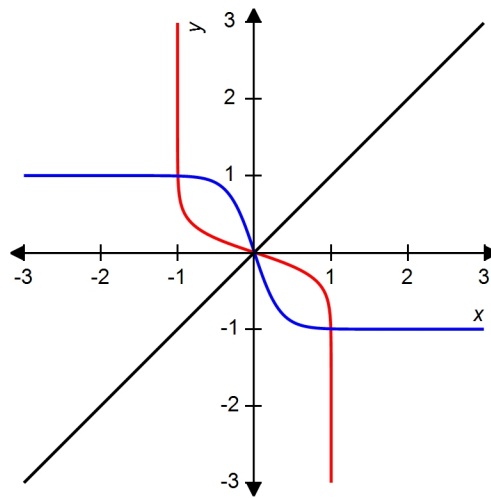
ANSWER: d
 POINTS: 1
 DIFFICULTY: Easy
 REFERENCES: 1.6.31
 QUESTION TYPE: Multi-Mode (Multiple choice)
 HAS VARIABLES: True
 STUDENT ENTRY MODE: Basic
 LEARNING OBJECTIVES: PCALC.CO.H.LO.01.05.10 - Find the inverse of a function algebraically.
 KEYWORDS: 7ET
 OTHER: Bimodal
 NOTES: Section 1.6
 DATE CREATED: 7/20/2015 1:46 PM
 DATE MODIFIED: 2/10/2020 12:40 AM

1.5 Logarithms

7. Find the inverse of f . Then use a graphing utility to plot the graphs of f and f^{-1} on the same set of axes.

$$f(x) = \frac{1 - e^{6x}}{1 + e^{6x}}$$

ANSWER:
$$f^{-1}(x) = \frac{1}{6} \ln \left(\frac{1 - x}{1 + x} \right)$$



POINTS:	1
DIFFICULTY:	Medium
REFERENCES:	1.6.26
QUESTION TYPE:	Subjective Short Answer
HAS VARIABLES:	True
STUDENT ENTRY MODE:	Basic
LEARNING OBJECTIVES:	PCALC.CO.H.LO.03.02.09 - Graph logarithmic functions involving common and natural logarithms using a graphing tool.
KEYWORDS:	7ET
OTHER:	Short Answer
NOTES:	Section 1.6
DATE CREATED:	7/20/2015 1:46 PM
DATE MODIFIED:	2/10/2020 12:42 AM

1.5 Logarithms

8. Find the domain, range, and x -intercept(s) of the function.

$$f(x) = \ln(x - 4) - 1$$

ANSWER: Domain: $(4, \infty)$ Range: $(-\infty, \infty)$ x -intercept: $x = e + 4$

POINTS: 1
DIFFICULTY: Medium
REFERENCES: 1.6.50
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.03.02.05 - Find the domain and range of logarithmic functions.
KEYWORDS: 7ET
OTHER: Numerical Response
NOTES: Section 1.6
DATE CREATED: 7/20/2015 1:46 PM
DATE MODIFIED: 1/30/2020 7:11 AM

1.5 Logarithms

9. Use the laws of logarithms to expand the expression.

$$\ln\left(\frac{x+1}{x-2}\right)^{\frac{1}{2}}$$

a. $\frac{1}{2}\ln[(x+1)(x-2)]$

b. $\frac{1}{2}\ln(x+1) - \frac{1}{2}\ln(x-2)$

c. $\frac{1}{2}\ln\left(x - \frac{1}{2}\right)$

d. $\frac{1}{2}\ln\left(\frac{x+1}{x-2}\right)$

ANSWER: b

POINTS: 1

DIFFICULTY: Easy

REFERENCES: 1.6.39

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.03.03.06 - Expand logarithmic expressions using the laws of logarithms.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: Section 1.6

DATE CREATED: 7/20/2015 1:46 PM

DATE MODIFIED: 1/30/2020 6:17 AM

1.5 Logarithms

10. Use the laws of logarithms to write the expression as the logarithm of a single quantity.

$$4 \ln 5 - \frac{3}{4} \ln(x + 3)$$

a. $\ln \frac{625}{(x + 3)^{3/4}}$

b. $\frac{4 \ln 5}{\frac{3}{4} \ln(x + 3)}$

c. $\ln 5^4 - \ln(x + 3)^{3/4}$

d. $\frac{3 \ln 625}{4(x + 3)}$

ANSWER: a

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 1.6.40

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.03.03.07 - Combine logarithmic expressions using the laws of logarithms.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: Section 1.6

DATE CREATED: 7/20/2015 1:46 PM

DATE MODIFIED: 1/30/2020 6:23 AM

1.5 Logarithms

11. Simplify the expression.

$$e^{3\ln 4}$$

- a. 7
- b. 12
- c. 64
- d. 81

ANSWER: c
POINTS: 1
DIFFICULTY: Easy
REFERENCES: 1.6.38a
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.03.03.05 - Rewrite the logarithm of a power using the laws of logarithms.
KEYWORDS: 7ET
OTHER: Bimodal
NOTES: Section 1.6
DATE CREATED: 7/20/2015 1:46 PM
DATE MODIFIED: 1/30/2020 6:47 AM

1.5 Logarithms

12. Solve the equation.

$$3e^{x+2} = 2$$

a. $x = \ln \frac{2}{3} - 2$

b. $x = \ln \frac{2}{3} + 2$

c. $x = \ln \frac{3}{2} - 2$

d. $x = \ln \frac{3}{2} + 2$

ANSWER: a

POINTS: 1

DIFFICULTY: Easy

REFERENCES: 1.6.51a

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.CO.H.LO.03.04.04 - Solve exponential equations using logarithms.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: Section 1.6

DATE CREATED: 7/20/2015 1:46 PM

DATE MODIFIED: 2/5/2020 5:51 AM

1.5 Logarithms

13. Find a formula for the inverse of the function.

$$y = \ln(x + 8)$$

a. $y = e^x - 8$

b. $y = e^x + 8$

c. $y = -8e^x$

d. $y = 8e^x$

e. $y = e^{x+8}$

ANSWER: a

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 1.6.25

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.01.05.10 - Find the inverse of a function algebraically.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: Section 1.6

DATE CREATED: 7/20/2015 1:46 PM

DATE MODIFIED: 1/30/2020 6:51 AM

1.5 Logarithms

14. Find the exact value of the expression.

$$\log_5 100 + \log_5 50 - 3\log_5 2$$

- a. 7
- b. 8
- c. 6
- d. 4
- e. 5

ANSWER: d
POINTS: 1
DIFFICULTY: Medium
REFERENCES: 1.6.37a
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: PCALC.COH.LO.03.03.02 - Evaluate logarithms using the laws of logarithms.
KEYWORDS: 7ET
OTHER: Bimodal
NOTES: Section 1.6
DATE CREATED: 7/20/2015 1:46 PM
DATE MODIFIED: 1/30/2020 6:53 AM

1.5 Logarithms

15. If $f(x) = 3x + \ln x$, find $f^{-1}(3)$. Round to the nearest whole.

ANSWER: $f^{-1}(3) = 1$

POINTS: 1
DIFFICULTY: Medium
REFERENCES: 1.6.17
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.LO.01.05.09 - Evaluate the inverse of a one-to-one function given its numerical, algebraic, or graphical representation.
KEYWORDS: 7ET
OTHER: Numerical Response
NOTES: Section 1.6
DATE CREATED: 7/20/2015 1:46 PM
DATE MODIFIED: 1/30/2020 6:58 AM

16. Solve each equation for x .

(a) $\ln x = 3$ (b) $e^{e^x} = 6$

ANSWER: $x = e^3, x = \ln(\ln 6)$

POINTS: 1
DIFFICULTY: Medium
REFERENCES: 1.6.51
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
LEARNING OBJECTIVES: PCALC.COH.UO.03.04.04 - Solve exponential and logarithmic equations algebraically and graphically.
KEYWORDS: 7ET
OTHER: Numerical Response
NOTES: Section 1.6
DATE CREATED: 7/20/2015 1:46 PM
DATE MODIFIED: 1/30/2020 7:00 AM

1.5 Logarithms

17. When a camera flash goes off, the batteries immediately begin to recharge the flash's capacitor, which stores electric charge given by

$$Q(t) = Q_0(1 - e^{-t/a})$$

(The maximum charge capacity Q_0 is and t is measured in seconds.) How long does it take to recharge the capacitor to 90% of capacity if $a = 4$?

a. $-4\ln\left(\frac{9}{10}\right)$ seconds

b. $-4\ln\left(\frac{1}{10}\right)$ seconds

c. $-4\ln(10)$ seconds

d. $-4\ln(1)$ seconds

e. $-\ln\left(\frac{4}{9}\right)$ seconds

ANSWER: b

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 1.6.62b

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.CO.H.LO.03.01.10 - Solve applied problems involving exponential functions.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: Section 1.6

DATE CREATED: 7/20/2015 1:46 PM

DATE MODIFIED: 1/30/2020 6:56 AM

1.5 Logarithms

18. Suppose that the graph of $y = \log_2 x$ is drawn on a coordinate grid where the unit of measurement is an inch. How many miles to the right of the origin do we have to move before the height of the curve reaches 3 ft? Rounded to the nearest mile.

- a. 5.2 mi
- b. 1,084,587.7 mi
- c. 103 mi
- d. 13,015,052.4 mi
- e. -97 mi

ANSWER: b

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 1.6.45

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.CO.H.LO.03.04.07 - Solve logarithmic equations using the laws of logarithms.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: Section 1.6

DATE CREATED: 7/20/2015 1:46 PM

DATE MODIFIED: 1/30/2020 4:53 AM

1.5 Logarithms

19. If a bacteria population starts with 100 bacteria and doubles every three hours, then the number of bacteria after t hours is

$$n = f(t) = 100\left(2^{\frac{t}{3}}\right).$$

When will the population reach 45,000? Round the answer to the nearest tenth.

- a. 26.4 hours
- b. 16.4 hours
- c. 31.4 hours
- d. 21.4 hours
- e. 36.4 hours

ANSWER: a

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 1.6.61b

QUESTION TYPE: Multi-Mode (Multiple choice)

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.03.01.10 - Solve applied problems involving exponential functions.

KEYWORDS: 7ET

OTHER: Bimodal

NOTES: Section 1.6

DATE CREATED: 7/20/2015 1:46 PM

DATE MODIFIED: 1/30/2020 4:58 AM

1.6 Sequences and Difference Equations

1. Write the first five terms of the sequence $\{a_n\}$ whose n^{th} term is given.

$$a_n = \frac{n+9}{5n-1}$$

ANSWER: $\frac{5}{2}, \frac{11}{9}, \frac{6}{7}, \frac{13}{19}, \frac{7}{12}$

POINTS: 1

DIFFICULTY: Easy

REFERENCES: 11.1.3

QUESTION TYPE: Subjective Short Answer

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.10.01.04 - Find the n th term of a sequence.

OTHER: Short Answer

NOTES: Section 11.1

DATE CREATED: 7/20/2015 2:26 PM

DATE MODIFIED: 2/7/2020 9:08 AM

2. Find a formula for the general term a_n of the sequence, assuming that the pattern of the first few terms continues.

$$\left\{ -\frac{1}{2}, \frac{8}{3}, -\frac{27}{4}, \frac{64}{5}, -\frac{125}{6}, \dots \right\}$$

ANSWER: $a_n = \frac{(-1)^n n^3}{n+1}$

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 11.1.17

QUESTION TYPE: Numeric Response

HAS VARIABLES: True

LEARNING OBJECTIVES: PCALC.COH.LO.10.01.07 - Write a formula for the n th term of a given sequence.

OTHER: Numerical Response

NOTES: Section 11.1

DATE CREATED: 7/20/2015 2:26 PM

DATE MODIFIED: 2/11/2020 3:14 AM

1.6 Sequences and Difference Equations

3. Find an expression for the n^{th} term of the sequence. (Assume that the pattern continues.)

$$\left\{ \frac{5}{4}, \frac{10}{9}, \frac{15}{16}, \frac{20}{25}, \frac{25}{36}, \dots \right\}$$

ANSWER:
$$a_n = \frac{5n}{(n+1)^2}$$

POINTS: 1

DIFFICULTY: Medium

REFERENCES: 11.1.13

QUESTION TYPE: Subjective Short Answer

HAS VARIABLES: True

STUDENT ENTRY MODE: Basic

LEARNING OBJECTIVES: PCALC.COH.LO.10.01.07 - Write a formula for the n th term of a given sequence.

OTHER: Short Answer

NOTES: Section 11.1

DATE CREATED: 7/20/2015 2:26 PM

DATE MODIFIED: 2/11/2020 3:18 AM

1.6 Sequences and Difference Equations

4. A sequence $\{a_n\}$ is defined recursively by the equation $a_n = 0.5(a_{n-1} + a_{n-2})$ for $n \geq 3$ where $a_1 = 18, a_2 = 18$.

Use your calculator to guess the limit of the sequence.

- a. 6
- b. 18
- c. 26
- d. 17
- e. 19

ANSWER: b
POINTS: 1
DIFFICULTY: Medium
REFERENCES: 11.2.88
QUESTION TYPE: Multi-Mode (Multiple choice)
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: CALC.COH.LO.07.01.01 - Find the limit of a sequence.
OTHER: Bimodal
NOTES: Section 11.2
DATE CREATED: 7/20/2015 2:26 PM
DATE MODIFIED: 7/10/2020 3:18 PM

5. A sequence $\{a_n\}$ is defined recursively by the equation $a_n = 0.5(a_{n-1} + a_{n-2})$ for $n \geq 3$ where $a_1 = 20, a_2 = 20$. Use your calculator to guess the limit of the sequence.

ANSWER: 20
POINTS: 1
DIFFICULTY: Medium
REFERENCES: 11.2.88
QUESTION TYPE: Numeric Response
HAS VARIABLES: True
OTHER: Numerical Response
NOTES: Section 11.2
DATE CREATED: 7/20/2015 2:26 PM
DATE MODIFIED: 2/10/2020 7:24 AM

1.6 Sequences and Difference Equations

6. An annuity is a sequence of payments made at regular intervals. Suppose that a sum of \$150 is deposited at the end of each month into an account earning interest at the rate of 12% per year compounded monthly. Then the amount on deposit at the end of the n^{th} month is $f(n) = 15,000[(1.01)^n - 1]$.

Consider the sequence $\{a_n\}$ defined by $a_n = f(n)$.

(a) Find the 24th term of the sequence, and interpret your result.

(b) Evaluate $\lim_{n \rightarrow \infty} a_n$, and interpret your result.

ANSWER: (a) \$4,046.02 -- This is the amount on deposit after 24 months.
(b) ∞ -- The amount on deposit will increase indefinitely as the number of months of deposits increased indefinitely.

POINTS: 1
DIFFICULTY: Medium
REFERENCES: 11.1.65
QUESTION TYPE: Subjective Short Answer
HAS VARIABLES: True
STUDENT ENTRY MODE: Basic
LEARNING OBJECTIVES: CALC.COH.LO.07.01.01 - Find the limit of a sequence.
OTHER: Short Answer
NOTES: Section 11.1
DATE CREATED: 7/20/2015 2:26 PM
DATE MODIFIED: 2/7/2020 9:25 AM